

# Preparing to Learn from Math Instruction

Mastery-Oriented Students Benefit Most  
from Exploratory Activities

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Should children  
be taught new  
concepts  
directly...



or discover  
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# Direct Instruction

Should children be taught new concepts directly...



# Discovery Learning

or discover these ideas for themselves?

# Direct Instruction



# Discovery Learning

# Direct Instruction

Lessens burden  
on cognitive  
resources

(Kirschner et al., 1996)



# Discovery Learning

Increases  
motivation and  
depth of  
understanding

(Wise & O' Neill, 2009)

# Direct Instruction

Lessens burden  
on cognitive  
resources

(Kirschner et al., 1996)



**How can aspects of both approaches be combined to improve learning?**



# Discovery Learning

Increases  
motivation and  
depth of  
understanding

(Wise & O' Neill, 2009)

# Exploratory Activities May Help Children Learn from Instruction

## Evidence

- College students who explored examples learned more deeply from a psychology lecture than those who summarized a text

(Schwartz & Bransford, 1998)

- 9<sup>th</sup> graders who explored datasets before instruction on descriptive statistics learned more from new instructional resources than those who received extended instruction

(Schwartz & Martin, 2004)

# Exploratory Activities May Help Children Learn from Instruction

## **Evidence**

- These benefits are most apparent for complex problems requiring new insight



# Individual Differences

Differences in how students respond to challenge may impact learning from exploratory experiences

Students approach learning with different goals and conceptions of “ideal” performance

(Hidi & Renninger, 2006)

# Individual Differences

## Students with **higher mastery-orientation**

- Motivated by a desire for personal growth
- Tend to view challenge (e.g., confusion, difficulty) as a signal there is an opportunity to learn and grow
- Generally respond to setbacks with increased effort and persistence
- Seek out challenge (e.g., new problem-solving experiences)

(Diener & Dweck, 1980)

# Individual Differences

## Students with **lower mastery-orientation**

- Do not especially appreciate the learning process itself (they want the answers)
- May even interpret challenge as signaling personal inadequacy and failure, causing them to withdraw from the activity

(Dweck & Leggett, 1988)

# Current Study

Examined whether exploratory experiences (solving novel math problems) helped children learn from instruction at a deeper level

Because of individual differences in response to challenge, we anticipated that exploration would be more beneficial for higher mastery-oriented children

# Math Equivalence

Operations on both sides of the equal sign represent the same quantity

$$3 + 4 = 3 + 4$$

Children often treat the equal sign operationally

$$3 + 4 = \boxed{7} + 4$$

- “It means add the numbers” or “get the answer”

Children need to have a relational view

- Look at relations across both sides of the equal sign

Important prerequisite for understanding algebra, even in early grades (NCTM, 2006)

# Instruction Conditions

## Order

- Instruct – Solve
- Solve – Instruct

## Hypotheses

- The Solve – Instruct order should improve conceptual knowledge (understanding at a deeper level)
- Mastery orientation should enhance this effect

Children with higher mastery orientation should be better equipped to deal with the challenge

# Procedure

## **Pretest**

- 2<sup>nd</sup>-4<sup>th</sup> graders
- Suburban public school
- Selected if scored < 80% on Math Equivalence Assessment
- $N = 159$

## **Intervention & Immediate Posttest**

## **Retention Test (after 2 weeks)**

# Mastery-Orientation Measure

Given at Pretest

Mastery-orientation score: Average of 2 items

- “In math class, I prefer course material that really challenges me so I can try new things”
- I want to learn as much as possible about math, even if I have to work hard.

1

Strongly  
Disagree

2

Disagree

3

Somewhat  
Disagree

4

Somewhat  
Agree

5

Agree

6

Strongly  
Agree

(Elliot, 1999)



# Math Equivalence Assessment

## Procedural knowledge

- Solving problems correctly

$$3 + 7 + 8 = 3 + \square$$

## Conceptual knowledge

- Understand concept of equivalence

Is  $4 + 8 = 8 + 4$  True or False?

What does the equal sign mean?

## Pretest

ES1. What does the equal sign (=) mean?

It means sum or difference.

## Retention

ES1. What does the equal sign (=) mean?

It means that 2 things are the same like a scale.

## Pretest

ES1. What does the equal sign (=) mean?

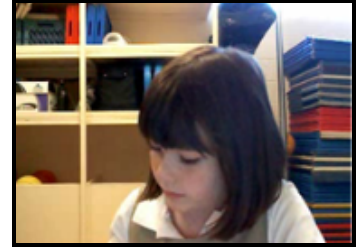
It tells the sum.  
ex.  $4 + 2 = 6$

## Retention

ES1. What does the equal sign (=) mean?

It means both sides are the same.

# Tutoring Intervention



## Conceptual Instruction

$$3 + 4 = 3 + 4$$

*There are two sides to this problem...*

*What the **equal sign** means is that the things on both sides of the equal sign are **equal** or **the same**...*

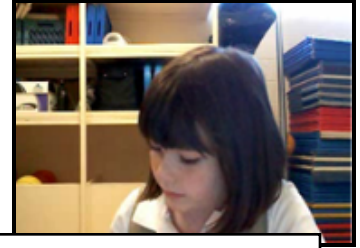
## Problem Solving

$$3 + 4 + 8 = \square + 8$$

How did you get your answer?

7 is the right answer.

# Tutoring Intervention



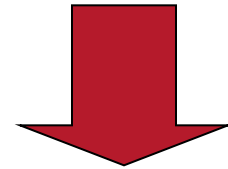
## Conceptual Instruction

$$3 + 4 = 3 + 4$$

*There are two sides to this problem...*

*What the **equal sign** means is that the things on both sides of the equal sign are **equal** or **the same**...*

**Instruct – Solve**



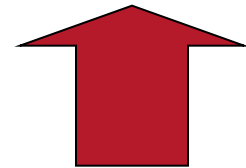
## Problem Solving

$$3 + 4 + 8 = \square + 8$$

How did you get your answer?

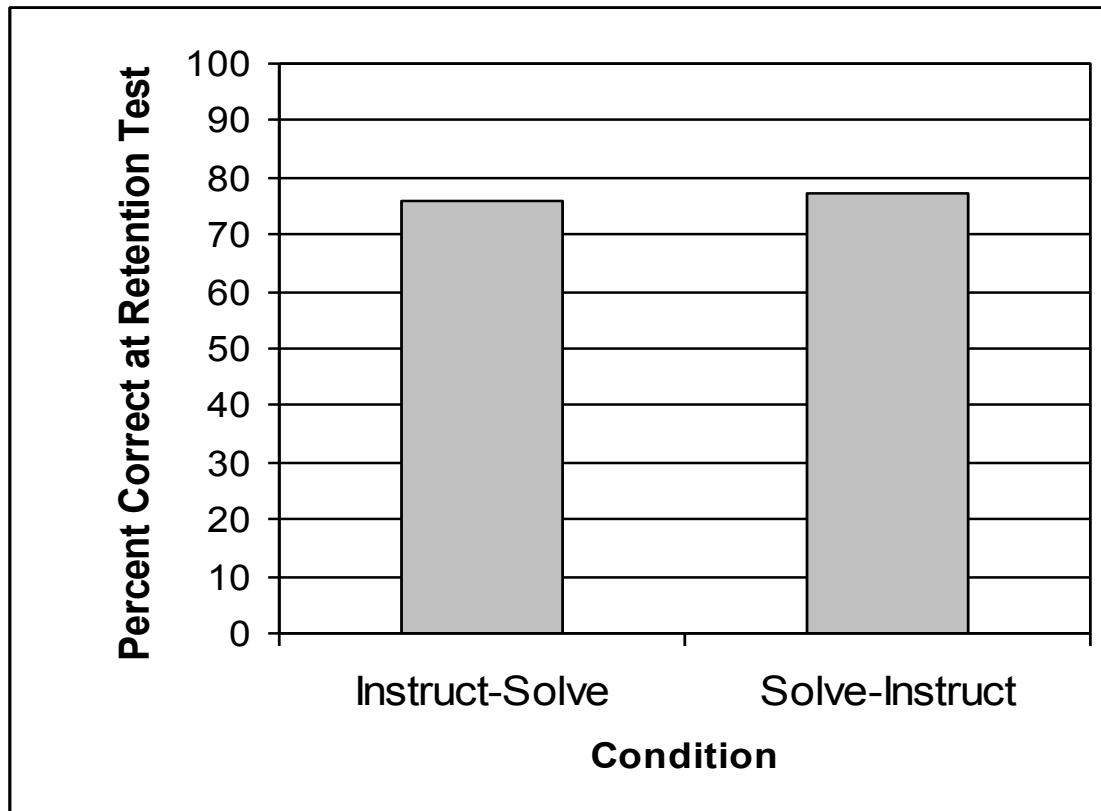
7 is the right answer.

**Solve – Instruct**



# Retention Test Results

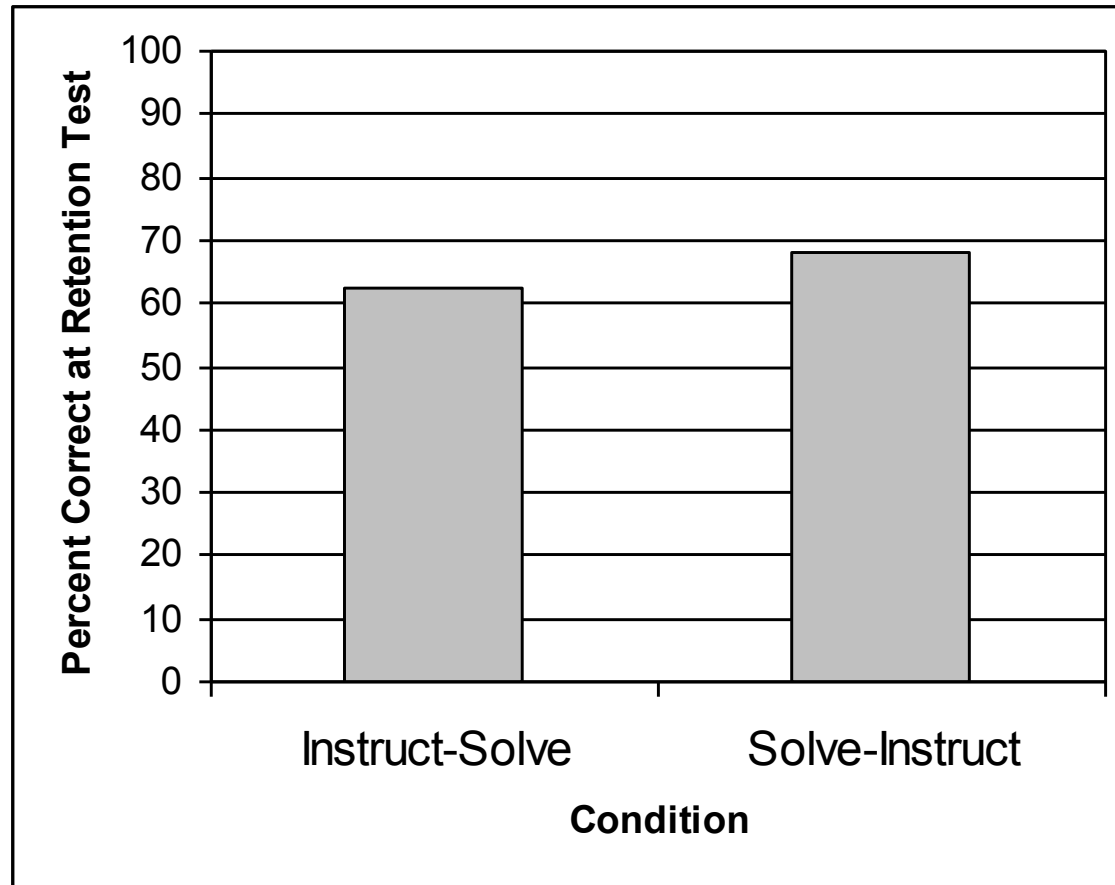
## Procedural Knowledge (Problem Solving)



**No effect of order or interaction**

# Retention Test Results

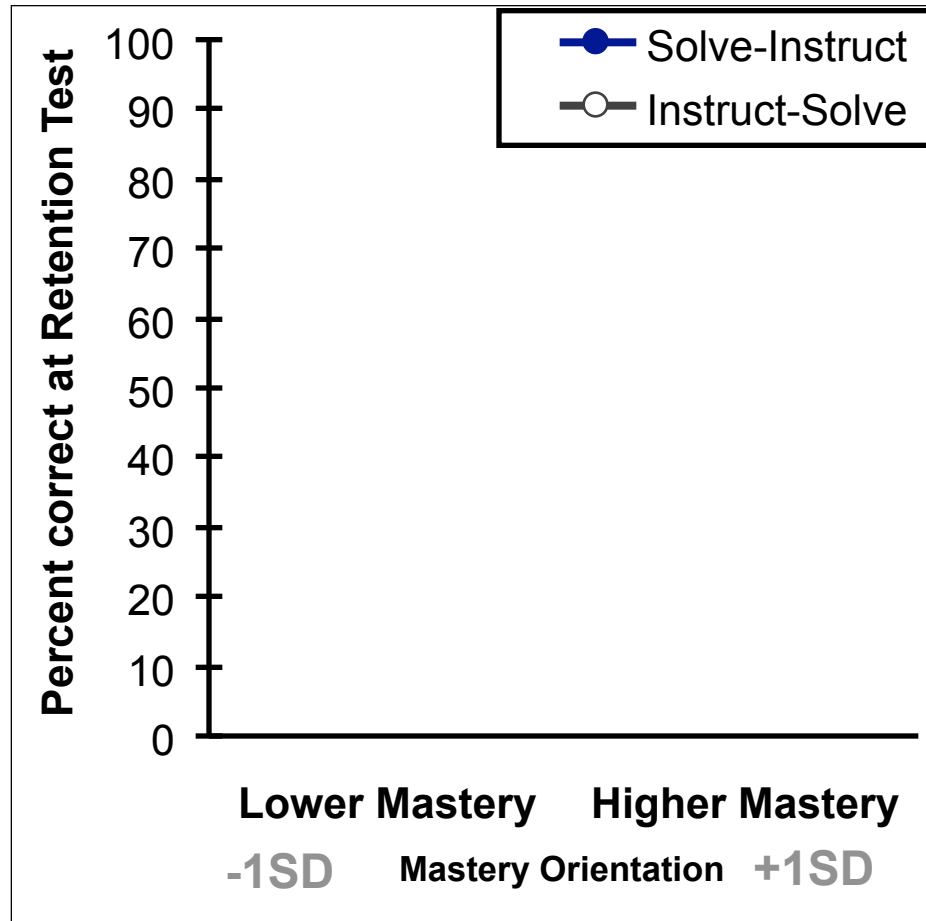
## Conceptual Knowledge



**Marginal effect of order,  $p < .08$**

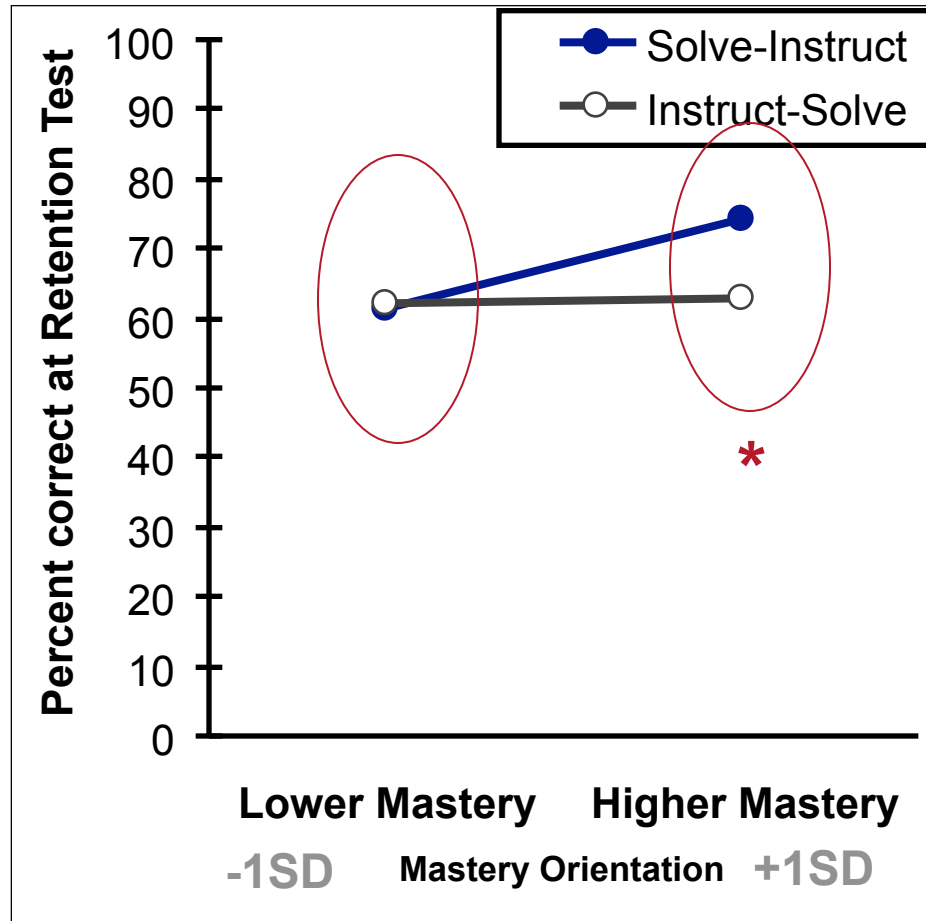
# Retention Test Results

## Conceptual Knowledge



# Retention Test Results

## Conceptual Knowledge





# Summary

Exploring problems before instruction improved subsequent conceptual knowledge...

...But only for children higher in mastery-orientation

- Discovery learning activities can be challenging
- Mastery-oriented children tend to be more resilient to such challenges, approaching such activities with the goal to master and understand the content

Lower-mastery orientation did not benefit learning, but it did not hurt either

# Conclusions

Overall, adding exploratory activities before instruction better than a conventional tell-then-practice approach

- One practical exploratory activity: Solve unfamiliar problems with feedback

Examines an important constraint

- Exploratory activities may be best suited for students who are most motivated for this type of challenge

Combines elements of discovery learning and direct instruction

- Joins a growing body of literature

(e.g., Schwartz & colleagues)

# Conclusions

Future research is needed

- To replicate these findings with a more comprehensive mastery-orientation scale or direct observation
- To extend these findings to the classroom, in other domains, and with other types of exploratory activities
- To see if supporting mastery-orientation allows all students to benefit from exploration

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