## EXAMINING THE ROLES OF PATTERNING KNOWLEDGE, SPATIAL ASSEMBLY,AND ANALOGIC REASONING IN EARLY MATHEMATICS DEVELOPMENT

SRCD BIENNIAL MEETING, APRIL, 202I, THU, APRIL 8, I0:00AM-II:30AM
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## EMPHASIZING THE NUMBERS IN PATTERNS DURING TRAINING: EFFECTS ON PATTERNING AND MATH SKILLS

## SRCD BIENNIAL MEETING, APRIL 2021

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## BACKGROUND

- Most early math research and theory has classically focused on the contributions of numeracy skills (Sarama \& Clements, 2009)

- Recent work focuses more broadly to include the contributions of early non-numeracy topics such as repeating patterning (e.g., Fyfe et al., 2019; Rittle-Johnson, Zippert, Boice, 2018; Wijns et al., 2019; Zippert et al., 2019; 2020)



## BACKGROUND

## - Gaps

- Is the patterning and math link causal?
- What is the mechanism through which patterning $\rightarrow$ mathematics knowledge?
- Patterning $\rightarrow$ Numeracy $\rightarrow$ Math
- Evidence that patterning and numeracy are correlated (Fyfe et al., 2017; Mackay \& De Smedt, 20I9; Wijns et al., 20I9; Zippert et al., 2019; 2020)
- Shared reliance on rules and regularities
- Numeracy
- Can rely on counting string to answer magnitude comparison problems ( 5 comes later in the count sequence than 3 , so 5 is bigger)
- The next number in the count sequence after 4 is 5 , so $4+1=5$ (successor principle; Gelman \& Gallistel, 1978; Sarnecka \& Carey, 2008)
- Patterns
- Reciting items in order in the pattern sequence helps to know what comes next
- Knowing the unit repeats over and over in the count sequence helps you determine what comes next


## AIMS

I. Can we improve repeating patterning skill in preschool through targeted instruction? Hypothesis I: Yes
2. Can we improve successor principle knowledge through targeted tutoring? Hypothesis 2:Yes
3. Can improving patterning along with numeracy promote numeracy and mathematics knowledge more than numeracy training alone?

Hypothesis 3:Yes

- 212 preschool children ( $M=4.7$ years, $S D=.37$ )
- Recruited from 12 preschools (5 public, 7 private)
- $56 \%$ male, $53 \%$ white, $10 \%$ bilingual
- $35 \%$ received some form of financial assistance for school
- 72 in patterning + numeracy, 70 in literacy + numeracy, 70 in control
- Additional 21 students dropped due to persistent non-compliance issues or missing 2 training sessions


## STUDY 2 DESIGN

- Participants randomly assigned to 3 conditions:
I. Repeating Patterning + Numeracy Instruction
a. Repeating patterning activities and Numeracy activity (successor principle) at end of each lesson

2. Literacy + Numeracy Instruction
a. Literacy activities so spend same time with experimenter and Numeracy activity (successor principle) at end of each lesson

## 3. Passive control group

a. Regular classroom instruction only

- Most patterning and numeracy activities modified from Building Blocks Pre-K curriculum
- Literacy activities taken from Opening the World of Learning (OWL) Prek-K curriculum



## MEASURES

## Teacher Patterning Measure Example Items



Research Patterning Measure Example Items


## Successor Principle: Fish Pond Task

- Assess children's knowledge of the successor principle using numbers ranging from 2 to 20 with 10 items ( 7 addition and 3 subtraction). Based on Cheung et al. (2017)

"Three fish are swimming under the lilypad. Now watch... another fish swims in! Now are there 4 or 5 fish?"


## MEASURES CONTINUED

Broad Math \& Numeracy Knowledge
The REMA Short-Form of Research-Based Early Mathematics Assessment (Clements \& Sarama, 2000; Weiland et al., 2012)

Numeracy example knowledge

| 1 | $\bullet$ |
| :---: | :---: |
| 2 | $\bullet$ |
| 3 | $\bullet \bullet$ |
| 4 | $\vdots!$ |
| 5 | $\ddots \bullet$ |

Shape example


## STUDY 2 DESIGN

## Pretest

## Post test <br> Day 1

## Post test <br> Day 2

Children are pretested in one 25 -minute session

- Math (REMA)
- Pattern: TeacherBased
- Successor

Principle: Fish
Pond

## Randomized to Condition

## Intervention

Children are first randomized to condition, and then assigned to a group of 2 based on varying pattern ability

Children in groups of 2 receive five 25 -minute training sessions across 2-3 weeks


The day after session 5, children are assessed in one 20-minute session

- Pattern:

Research-Based

- Successor

Principle


Within a few days of post day 1 , children are assessed in another 20-minute session

- Math (REMA)
- Pattern:

Teacher-Based

What's Next Pattern AB

"What comes next in the
pattern? Use one of these." [Experimenter gestures to response options.]

## OVERVIEW OF PATTERNING + NUMERACYTRAINING SESSIONS

| Session | Patterning Focus | Numeracy Focus (Successor Principle) |
| :---: | :--- | :--- |
| 1 | Duplicate and extend patterns | Add 1 (small numbers) |
| 2 | Duplicate and extend patterns | Add 1 (small numbers) |
| 3 | Identify core unit of patterns | Subtract 1 (small numbers) |
| 4 | Abstract patterns | Add 1 (large numbers and review small <br> numbers) |
| 5 | Review core unit of patterns and abstract <br> patterns | Add and subtract 1 (small and large numbers) |

## OVERVIEW OF LITERACY + NUMERACYTRAINING SESSIONS

| Session | Literacy Focus (OWL Unit 1 Week 2) | Numeracy Focus (Successor <br> Principle) |
| :---: | :--- | :--- |
| 1 | oral language, phonological awareness, alphabet knowledge, <br> concepts of print, motivation to read, listening comprehension | Add 1 (small numbers) |
| 2 | oral language, phonological awareness, alphabet knowledge | Add 1 (small numbers) |
| 3 | oral language, phonological awareness, alphabet knowledge | Subtract 1 (small numbers) |
| 4 | oral language, phonological awareness, | Add 1 (large numbers and <br> review small numbers) |
| 5 | oral language, concepts of print, motivation to read | Add and subtract 1 (small and <br> large numbers) |

## PRETEST RESULTS

## IRT Scores at Pretest by Training Condition

- Control

■ Literacy+Numeracy

- Patterning+Numeracy



## POSTTEST RESULTS

Teacher-based Pattern Scores by Training Condition


Research-based Pattern Scores by Training Condition


## Study 1 Hypotheses:

Children's repeating patterning knowledge can be improved through targeted instruction. (yes but aligned measure only)

## RESULTS

## Successor Principle Scores at Posttest by Training Condition



## Study 2 Hypotheses:

Hypothesis 2: Children's knowledge of the successor principle, a core early numeracy skill, can be improved through targeted instruction.

## POSTTEST RESULTS



## Study 3 Hypotheses:

Hypothesis 3: Improving children's repeating patterning knowledge prepares them to learn more from numeracy instruction on the successor principle, both on that skill and math more broadly.

## DISCUSSION

## Summary

- Patterning instruction improved patterning knowledge, but only on measure aligned with training and more focused on unit of repeat
- Instruction did not differentially improve math or numeracy and did not improve successor principle knowledge at all.
- In line with other studies with young children that did not find effects of training numeracy and nonnumeracy skills together (Barnes et al., 2016; Kroesbergen et al., 20I2; Kyttälä et al., 2015)
- Patterning + numeracy instruction may support other numeracy skills
- Knowledge of count sequence (what's before/after, but not highest count; Zippert et al., 2020)
- Ordinal knowledge (e.g., what number comes before 5)


## THE PATTERNING TEAM!



