

Question: Let x be a real number. Let $\lceil x \rceil$ be the smallest integer greater than x (ceiling), and $\lfloor x \rfloor$ be the largest integer less than x (floor). Prove that $\lceil x \rceil = \lfloor x \rfloor$ if and only if x is an integer.