

August 2019 Progress Update

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## Official Analysis Sample

- There were 771 students in our database from the Pre-K study, and the goal for the newly re-consented sample in 2013 was 500 students.
- THE FOLLOW-UP ANALYSIS SAMPLE CONSISTS OF 519 STUDENTS. o Middle School Follow-Up Study Time Points (IES and Heising Simons Foundation):
- Year 1 (5th grade): 517 students assessed
- Year 2 (6th grade): 513 students assessed
- Year 3 (7th grade): 503 students assessed
- Year 4 (8th grade): 496 students assessed
- Year 5 (9th grade): 486 students assessed
o High School Follow-Up Study Time Points (NSF):
- Year 1 (10 th grade): 457 students assessed

OVERVIEW OF STUDENT DIRECT ASSESMENT DATA COLLECTION

| Project Title | School Year | Grade Level ${ }^{*}$ | Assessment Timepoints |
| :---: | :---: | :---: | :---: |
| Building Blocks | 2007-2008 | Pre-K | T1 = Fall Pre-K |
|  |  |  | T2 = Spring Pre-K |
|  | 2008-2009 | Kindergarten | T3 = Spring K* |
|  | 2009-2010 | $1{ }^{\text {st }}$ | T4 = Spring $1^{\text {st }}$ Grade* |
| "Between Study Years" | 2010-2011 | $2^{\text {nd }}$ | $N / A$ |
|  | 2011-2012 | $3^{\text {rd }}$ | $N / A$ |
|  | 2012-2013 | $4^{\text {th }}$ | $N / A$ |
| Middle School Follow-Up Study | 2013-2014 | $5^{\text {th }}$ | T5 = Spring 5 ${ }^{\text {th }}$ Grade* |
|  | 2014-2015 | $6^{\text {th }}$ | T6 = Spring 6 ${ }^{\text {th }}$ Grade* |
|  | 2015-2016 | $7^{\text {th }}$ | T7 = Spring $7^{\text {th }}$ Grade* |
|  | 2016-2017 | $8^{\text {th }}$ | T8 = Spring 8 ${ }^{\text {th }}$ Grade* |
|  | 2017-2018 | 9th | T9 = Spring 9 ${ }^{\text {th }}$ Grade* |
| High School Follow-Up Study | 2018-2019 | $10^{\text {th }}$ | T10 = Spring 10 ${ }^{\text {th }}$ Grade* |
|  | 2019-2020 | $11^{\text {th }}$ | T11 = Spring 11 ${ }^{\text {th }}$ Grade* |
|  | 2020-2021 | $12^{\text {th }}$ | T12 = Spring $12^{\text {th }}$ Grade* |

[^0]
## Consort Chart: From the Original Study through the Follow-Up Studies



## Assessed Students in Grade 10



Note. "Other" schools include 1 that only serves students with IEPs, 1 K-12 school, 2 alternative schools, 1 school serving grades $7-12$, and 4 students who were homeschooled.
Note. This year, 77 students ( $17 \%$ of the assessed sample) were retained and were in $9^{\text {th }}$ grade.

## Mobility of Students between Schools in Grade 10

|  | Frequency | Percent |
| :--- | :---: | :---: |
| Attended 1 School | 414 | 90.6 |
| Attended 2 Schools | 33 | 7.2 |
| Attended 3 Schools | 10 | 2.2 |

Note. 15 of the students assessed this year ( $3.3 \%$ of the assessed sample) attended an alternative school at some point during the year.

## School Enrollment across Years

|  |  | Attended MNPS School |  | Did Not Attend MNPS School |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Year | N | Freq | Pct | Freq | Pct |
| Year 1 | 519 | 519 | 100.0 | 0 | 0.0 |
| Year 2 | 513 | 508 | 99.0 | 5 | 1.0 |
| Year 3 | 503 | 483 | 96.0 | 20 | 4.0 |
| Year 4 | 496 | 460 | 92.7 | 36 | 7.3 |
| Year 5 | 485 | 432 | 89.1 | 53 | 10.9 |
| Year 6 | 457 | 396 | 86.7 | 67 | 13.3 |

## DCS Custody across Years

| Year | \# Students in DCS Custody |
| :--- | :---: |
| $5^{\text {th }}$ Grade | 0 |
| $6^{\text {th }}$ Grade | 0 |
| $7^{\text {th }}$ Grade | 0 |
| $8^{\text {th }}$ Grade | 6 |
| $9^{\text {th }}$ Grade | 7 |
| $10^{\text {th }}$ Grade | 12 |

Note. We have documentation that the students listed in the above table were in DCS (TN Department of Children's Services) custody at some point during the respective school year.

## Demographic Information (Assessed Sample for Grade 10)

|  | $\mathbf{N}$ | Min | Max | Mean | SD |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Age at Time of Testing (in years) | 457 | 15.33 | 17.42 | 15.96 | .333 |
| PK Building Blocks Treatment | 281 | 15.33 | 17.42 | 15.93 | .328 |
| PK Control Condition | 176 | 15.42 | 17.17 | 16.01 | .318 |


|  | Overall |  | PK Building Blocks |  | PK Control |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Freq | Pct | Freq | Pct | Freq | Pct |
| Ethnicity |  |  |  |  |  |  |
| Black | 362 | 79.2 | 229 | 81.5 | 133 | 75.6 |
| White | 34 | 7.4 | 17 | 6.0 | 17 | 9.7 |
| Hispanic | 41 | 9.0 | 20 | 7.1 | 21 | 11.9 |
| Other | 20 | 4.4 | 15 | 5.3 | 5 | 2.8 |
| Gender |  |  |  |  |  |  |
| Male | 197 | 43.1 | 124 | 44.1 | 73 | 41.5 |
| Female | 260 | 56.9 | 157 | 55.9 | 103 | 58.5 |
| Number of Current Schools | 58 | - | 42 | - | 44 | - |
| Pre-K School System |  |  |  |  |  |  |
| Head Start (MAC) | 183 | 40.0 | 131 | 46.6 | 52 | 29.5 |
| MNPS Pre-K | 274 | 60.0 | 150 | 53.4 | 124 | 70.5 |

Note. Most students were located in Davidson County, but we also assessed any student who had moved to a contiguous county ( 2 in Cheatham, 15 in Clarksville-Montgomery, 4 in Robertson, 16 in Rutherford, 7 in Sumner, 2 in Williamson, and 6 in Wilson). In addition, 5 students attended a private school, and 4 were homeschooled.

## Socioeconomic Information

In the fall of 2018, when most students were in $10^{\text {th }}$ grade, 411 parents ( $79.2 \%$ ) were reinterviewed by phone to determine current education and income. Responses to questions regarding attitudes toward math and science are presented in the Appendix, parent section.

| Highest Education of Caregiver |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | Female Caregiver |  |  | Male Caregiver |  |
|  | Frequency | Percent |  | Frequency | Percent |
| Less than high school | 67 | 16.3 |  | 35 | 8.5 |
| High school diploma/GED | 220 | 53.5 |  | 153 | 37.2 |
| Associates degree | 66 | 16.1 |  | 22 | 5.4 |
| Bachelor's degree | 26 | 6.3 |  | 29 | 7.1 |
| Graduate degree | 24 | 5.8 |  | 1 | 0.2 |
| Not applicable | 6 | 1.5 |  | 135 | 32.8 |
| Don't know | 2 | 0.5 |  | 36 | 8.8 |

Number of Adults and Children in the Student's Home

|  | N adults $\mathbf{1}^{1}$ |  |  | N children $^{2}$ |  |
| :--- | :---: | :---: | :--- | :---: | :---: |
|  | Frequency | Percent |  | Frequency | Percent |
| 1 | 174 | 42.5 |  | 104 | 25.4 |
| 2 | 158 | 38.6 |  | 131 | 32.0 |
| 3 | 56 | 13.7 |  | 75 | 18.3 |
| 4 | 18 | 4.4 |  | 54 | 13.2 |
| 5 or more | 3 | 0.7 |  | 46 | 11.2 |

Note ${ }^{1} .2$ parents refused to answer question \#3 (\# of adults in student's household).
Note ${ }^{2} .1$ parent chose not to answer question \#4 (\# of children in student's household).

| Approximate Total Household Income for the Past Year |  |  |
| :--- | :---: | :---: |
|  | Frequency | Percent |
| Less than $\$ 20,000$ | 128 | 31.1 |
| $\$ 20,000-\$ 34,000$ | 104 | 25.3 |
| $\$ 35,000-\$ 49,000$ | 75 | 18.2 |
| $\$ 50,000-\$ 64,000$ | 33 | 8.0 |
| $\$ 65,000-\$ 79,000$ | 16 | 3.9 |
| Over $\$ 80,000$ | 25 | 6.1 |
| Don't know | 18 | 4.4 |
| Prefer not to answer | 12 | 2.9 |

## Student Outcomes: CMAT

From $5^{\text {th }}$ through $9^{\text {th }}$ grades, the project used KeyMath to assess students. During the 2018-2019 school year, after extensive piloting, we chose to switch to CMAT. The subscale scores in CMAT are somewhat different, but it does include both an Algebra and Geometry subtest. Instead of the KeyMath Numeration, CMAT has a Problem Solving subtest. We continued to give the Woodcock Johnson Quantitative Concepts subtest.

| CMAT |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Actual - <br> Expected <br> Mean |  |  |  |  |  |  |  |
| CMAT: Problem Solving |  |  |  |  |  |  |  |
| Age-Based Standard Score | 457 | 1.0 | 15.0 | 7.7 | 8.0 | 3.0 | -2.3 |
| Age Equivalent Score | 457 | 6.3 | 18.0 | 13.0 | 11.6 | 3.3 | -2.9 |
| Grade Equivalent Score | 457 | 1.2 | 12.7 | 7.8 | 6.4 | 3.2 | -2.9 |
| CMAT: Algebra |  |  |  |  |  |  |  |
| Age-Based Standard Score | 457 | 1.0 | 17.0 | 7.0 | 7.0 | 3.2 | -3.0 |
| Age Equivalent Score | 457 | 8.3 | 18.3 | 13.1 | 13.0 | 3.1 | -2.8 |
| Grade Equivalent Score | 457 | 3.2 | 12.7 | 7.9 | 8.0 | 3.1 | -2.8 |
| CMAT: Geometry |  |  |  |  |  |  |  |
| Age-Based Standard Score | 457 | 1.0 | 16.0 | 7.0 | 6.0 | 2.9 | -3.0 |
| Age Equivalent Score | 457 | 8.3 | 18.3 | 12.9 | 12.6 | 2.6 | -3.0 |
| Grade Equivalent Score | 457 | 3.2 | 12.7 | 7.7 | 7.4 | 2.5 | -3.0 |

Note. The average age of the students at testing was 15.9 years. The average current grade level of the students was 10.7.

## Student Outcomes: Woodcock-Johnson Subtests

| Quantitative Concepts | N | Min | Max | Mean | Median | SD |
| :--- | :--- | ---: | ---: | ---: | ---: | :---: |
| W-Score | 456 | 458.00 | 560.00 | 516.23 | 515.00 | 15.17 |
| Standard Score | 456 | 32.00 | 121.00 | 84.27 | 83.00 | 13.44 |

Note. We dropped Woodcock-Johnson data for 1 student this year due to assessor error.

## Woodcock-Johnson Scores across Years

- From the original Building Blocks study through this year, there were 10 testing time points. They were: fall of PK, spring of PK, spring of K, spring of $1^{\text {st }}$ grade, and spring of $5^{\text {th }}, 6^{\text {th }}, 7^{\text {th }}, 8^{\text {th }}, 9^{\text {th }}$, and $10^{\text {th }}$ grades.
- Letter-Word Identification was only given in fall of PK, spring of PK, spring of K, spring of $1^{\text {st }}$ grade, and spring of $7^{\text {th }}$ and $8^{\text {th }}$ grades.
- The graphs below show the scores over time for those 399 students who were tested at all possible time points.




## Student Direct Assessment Outcomes by School Type

|  | CHARTER |  | HIGH |  | OTHER |  | PRIVATE |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
|  | N | Mean | N | Mean | N | Mean | N |  |
| WJ QC (standard score) | 63 | 88.22 | 364 | 83.15 | 24 | 89.87 | 5 |  |
| CMAT PS (age-based standard score) | 63 | 8.79 | 365 | 7.37 | 24 | 8.67 | 5 |  |
| CMAT Alg (age-based standard score) | 63 | 8.06 | 365 | 6.67 | 24 | 8.71 | 5 |  |
| CMAT Geo (age-based standard score) | 63 | 7.70 | 365 | 6.81 | 24 | 8.25 | 5 |  |

Note. The "high school" category includes both MNPS high schools and out-of-county high schools.

## Connecting KeyMath and CMAT

KeyMath tops out at $10^{\text {th }}$ grade. Consequently, we changed assessment instruments in the 2018-2019 school year to CMAT. Because we changed assessment instruments, we assessed a sample of children to receive CMAT and one of the KeyMath subtests. To choose the students, we divided them into quartiles based on their past KeyMath performance. Within each quartile, we randomly assigned students to one of the KeyMath subtests. We lost students from some of the KeyMath assessments because of time issues or not being assessed this year. The following table presents results from children who were assessed with both KeyMath and CMAT in 2019. They served as a validation sample for our change of outcome measures; each child in the table below just completed one KeyMath subtest this year.

| KeyMath Subtest | N | Min | Max | Mean | Median | SD | Actual - <br> Expected <br> Mean |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| KeyMath: Numeration <br> Age-Scaled Score | 110 | 1.0 | 14.0 | 7.0 | 7.0 | 2.47 | -3.0 |
| Grade Equivalent | 110 | 1.2 | 10.0 | 6.2 | 6.0 | 2.40 | -4.5 |
| KeyMath: Algebra |  |  |  |  |  |  |  |
| Age-Scaled Score <br> Grade Equivalent | 115 | 1.0 | 13.0 | 7.4 | 7.0 | 3.06 | -2.6 |
| KeyMath: Geometry | 115 | 0.8 | 10.0 | 6.4 | 6.0 | 2.71 | -4.3 |
| Age-Scaled Score | 123 | 3.0 | 14.0 | 7.6 | 8.0 | 2.36 | -2.4 |
| Grade Equivalent | 123 | 1.5 | 10.0 | 6.6 | 7.0 | 2.46 | -4.1 |

Note. The average age of the students at testing was 16.0 years. The average current grade level of the students was 10.7.

## KeyMath Scores across Years

The following tables show students' KeyMath scores over time, from $5^{\text {th }}$ to $10^{\text {th }}$ grade and correlations with CMAT. Because each student only completed one KeyMath subtest this year, we restricted the sample for each subtest to students who had data for that subtest at all six assessment timepoints.

KeyMath Age-Scaled Scores across Years

| Year | Test | $\mathbf{N}$ | Mean | SD | Actual - Expected Mean |
| :--- | :--- | :---: | :---: | :---: | :---: |
| $5^{\text {th }}$ Grade | Numeration | 107 | 7.42 | 2.48 | -2.58 |
|  | Algebra | 111 | 8.04 | 2.85 | -1.96 |
|  | Geometry | 118 | 8.03 | 2.41 | -1.97 |
| 6 $^{\text {th }}$ Grade | Numeration | 107 | 7.60 | 2.48 | -2.40 |
|  | Algebra | 111 | 8.10 | 2.91 | -1.90 |
|  | Geometry | 118 | 7.80 | 2.39 | -2.20 |
| $7^{\text {th }}$ Grade | Numeration | 107 | 7.74 | 2.79 | -2.26 |
|  | Algebra | 111 | 8.20 | 2.98 | -1.80 |
|  | Geometry | 118 | 7.80 | 2.32 | -2.20 |
| 8th $^{\text {th }}$ Grade | Numeration | 107 | 7.27 | 2.62 | -2.73 |
|  | Algebra | 111 | 7.96 | 3.16 | -2.04 |
|  | Geometry | 118 | 8.01 | 2.64 | -1.99 |
| 9th $^{\text {th }}$ Grade | Numeration | 107 | 7.21 | 2.33 | -2.79 |
|  | Algebra | 111 | 7.88 | 3.07 | -2.12 |
|  | Geometry | 118 | 7.70 | 2.66 | -2.30 |
| 10 th Grade | Numeration | 107 | 7.07 | 2.50 | -2.93 |
|  | Algebra | 111 | 7.44 | 3.05 | -2.56 |
|  | Geometry | 118 | 7.64 | 2.39 | -2.36 |

Correlations Between $10^{\text {th }}$ Grade KeyMath and CMAT Scores

|  | I. KM <br> NUM | II. KM <br> ALG | III. KM <br> Geo | IV. CMAT <br> PS | V. CMAT <br> ALG | VI. CMAT <br> GEO |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| I. KeyMath Number (Age-Scaled) |  |  |  |  |  |  |
| II. KeyMath Algebra (Age-Scaled) | N/A |  |  |  |  |  |
| III. KeyMath Geometry (Age-Scaled) | N/A | N/A |  |  |  |  |
| IV. CMAT Problem Solving (Std. Score) | 0.76 | 0.82 | 0.68 |  |  |  |
| V. CMAT Algebra (Std. Score) | 0.59 | 0.85 | 0.62 | 0.66 |  |  |
| VI. CMAT Geometry (Std. Score) | 0.63 | 0.67 | 0.61 | 0.57 | 0.60 |  |

## Correlations between $9^{\text {th }}$ Grade KeyMath Assessments and TCAP/TNReady Scores

Each year, the project receives the state end of grade tests in the late fall of the year following spring testing. Consequently, for this report we can only examine the relations between the $9^{\text {th }}$ grade KeyMath assessments and the $9^{\text {th }}$ grade state tests. Tennessee switched its state test from the TCAP to TNReady in 2016.

Correlations Among Student Direct Assessment Scores \& TCAP/TNReady Scores across Years

|  | KeyMath Raw Scores |  |  |  |  |  |  |  |  |  |  |  | WJ Quant Concepts W Scores |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} \text { NUM } \\ \text { G5 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { NUM } \\ \text { G6 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { NUM } \\ \text { G8 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { NUM } \\ \text { G9 } \\ \hline \end{gathered}$ | $\begin{array}{\|c} \hline \text { ALG } \\ \text { G5 } \\ \hline \end{array}$ | $\begin{gathered} \hline \text { ALG } \\ \text { G6 } \\ \hline \end{gathered}$ | $\begin{array}{\|c} \hline \text { ALG } \\ \text { G8 } \\ \hline \end{array}$ | $\begin{gathered} \text { ALG } \\ \text { G9 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { Geo } \\ \text { G5 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { Geo } \\ \text { G6 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { Geo } \\ \text { G8 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { Geo } \\ \text { G9 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { WJQC } \\ \text { Y5 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { WJQC } \\ \text { Y6 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { WJQC } \\ \text { Y8 } \\ \hline \end{gathered}$ | $\begin{gathered} \text { WJQC } \\ \text { G9 } \\ \hline \end{gathered}$ |
| TCAP Math Scale Score 2013-2014 (5th Grade) | 0.63 | 0.69 | 0.69 | 0.67 | 0.62 | 0.66 | 0.69 | 0.67 | 0.45 | 0.56 | 0.56 | 0.56 | 0.57 | 0.60 | 0.64 | 0.64 |
| TCAP Math Scale Score 2014-2015 (6 ${ }^{\text {th }}$ Grade) | 0.61 | 0.66 | 0.68 | 0.65 | 0.60 | 0.67 | 0.70 | 0.68 | 0.49 | 0.57 | 0.58 | 0.58 | 0.55 | 0.60 | 0.66 | 0.66 |
| TNReady Math Scale Score 2016-2017 ( $8^{\text {th }}$ Grade) | 0.60 | 0.65 | 0.69 | 0.69 | 0.60 | 0.63 | 0.70 | 0.69 | 0.50 | 0.58 | 0.60 | 0.62 | 0.51 | 0.56 | 0.66 | 0.66 |
| TNReady Math Scale Score 2017-2018 (9 ${ }^{\text {th }}$ Grade) | 0.53 | 0.57 | 0.62 | 0.60 | 0.49 | 0.55 | 0.66 | 0.64 | 0.43 | 0.49 | 0.51 | 0.54 | 0.53 | 0.50 | 0.56 | 0.64 |

Note. All correlations are significant at the 0.01 level (2-tailed). Correlations between measures from the same year are bolded.

## Students' ${ }^{\text {th }}$ Grade Direct Assessment Scores within TCAP/TNReady Levels

In addition to a total score, the TNReady state test scores are divided into bands that characterize students as being below expected performance, approaching expectations, ontrack, or mastering the content area. We provide the mean scores for each band.

|  |  | KeyMath: Numeration <br> Age Scaled Score |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Perf. Level | N | Min | Max | Mean | SD |
| Below | 305 | 2.00 | 15.00 | 7.01 | 2.19 |
| Approaching | 60 | 4.00 | 15.00 | 9.27 | 2.07 |
| On-Track | 20 | 5.00 | 16.00 | 11.55 | 2.35 |
| Mastered | 6 | 10.00 | 19.00 | 13.67 | 3.20 |


|  |  | KeyMath: Algebra <br> Age Scaled Score |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Perf. Level | N | Min | Max | Mean | SD |
| Below | 305 | 1.00 | 13.00 | 7.29 | 2.38 |
| Approaching | 60 | 5.00 | 14.00 | 10.22 | 2.13 |
| On-Track | 20 | 7.00 | 17.00 | 11.95 | 2.28 |
| Mastered | 6 | 12.00 | 16.00 | 13.33 | 1.37 |


|  |  | KeyMath: Geometry <br> Age Scaled Score |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Perf. Level | N | Min | Max | Mean | SD |
| Below | 305 | 2.00 | 16.00 | 7.20 | 2.08 |
| Approaching | 60 | 4.00 | 15.00 | 9.33 | 2.40 |
| On-Track | 20 | 6.00 | 15.00 | 10.90 | 2.10 |
| Mastered | 6 | 10.00 | 15.00 | 12.17 | 1.72 |


|  |  | Woodcock-Johnson: |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Quantitative Concepts Standard Score |  |  |  |  |  |  |
| Perf. Level | N | Min | Max | Mean | SD |  |
| Below | 304 | 34.00 | 111.00 | 82.77 | 10.55 |  |
| Approaching | 60 | 69.00 | 112.00 | 93.92 | 9.13 |  |
| On-Track | 20 | 86.00 | 111.00 | 101.20 | 7.22 |  |
| Mastered | 6 | 96.00 | 121.00 | 110.83 | 8.91 |  |

Note. We dropped Quantitative Concepts data in the $9^{\text {th }}$ grade year for 1 student who was ill and had to leave school on the day she was tested.

## 9th Grade Direct Assessment Outcomes Within TNReady Levels






## Correlations among $10^{\text {th }}$ Grade Measures

|  | I. WJ QC | II. CMAT PS | III. CMAT ALG |
| :--- | :---: | :---: | :---: |
| I. WJ Quant Concepts (Std. Score) | -- | -- | -- |
| II. CMAT Problem Solving (Std. Score) | 0.73 | -- | -- |
| III. CMAT Algebra (Std. Score) | 0.73 | 0.66 | -- |
| IV. CMAT Geometry (Std. Score) | 0.66 | 0.57 | 0.60 |

Note. All correlations are significant at the 0.01 level (2-tailed).
Correlations among $9^{\text {th }} \& 10^{\text {th }}$ Grade Measures

|  |  | 9th Grade Outcomes |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{aligned} & \text { KM NUM } \\ & \text { (AGE-SCALED) } \end{aligned}$ | $\begin{aligned} & \text { KM ALG } \\ & \text { (AGE-SCALED) } \end{aligned}$ | $\begin{gathered} \text { KM GEO } \\ \text { (AGE-SCALED) } \end{gathered}$ | QCS |
| $\begin{aligned} & \text { On } \\ & 00 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | QCS | 0.82 | 0.83 | 0.68 | 0.86 |
|  | CMAT PS (STD SCORE) | 0.77 | 0.76 | 0.66 | 0.73 |
|  | CMAT ALG (STD SCORE) | 0.73 | 0.76 | 0.62 | 0.71 |
|  | CMAT GEO (STD SCORE) | 0.64 | 0.65 | 0.61 | 0.62 |

## Student Survey Outcomes: TIMSS (Trends in International Mathematics and Science Study) Math

Each year since $5^{\text {th }}$ grade, we have administered the TIMSS survey on math attitudes. This year we added the Science Survey. Students answered privately on paper.

|  | N | Min | Max | Mean | SD |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Confidence Scale Average | 457 | 1.25 | 4.00 | 2.92 | 0.67 |
| I know what my math teacher expects | 457 | 1.00 | 4.00 | 3.62 | 0.62 |
| My math teacher is easy to understand | 457 | 1.00 | 4.00 | 2.86 | 0.95 |
| I usually do well in math | 457 | 1.00 | 4.00 | 3.13 | 0.86 |
| Math is more difficult for me than my classmates (reverse coded) | 457 | 1.00 | 4.00 | 2.71 | 1.03 |
| Math is not one of my strengths (reverse coded) | 457 | 1.00 | 4.00 | 2.55 | 1.15 |
| I learn quickly in math | 457 | 1.00 | 4.00 | 2.76 | 0.96 |
| Math makes me confused and nervous (reverse coded) | 457 | 1.00 | 4.00 | 2.76 | 1.00 |
| I am good at working out hard math problems | 457 | 1.00 | 4.00 | 2.64 | 0.94 |
| My teacher thinks I am good at working out hard math problems | 457 | 1.00 | 4.00 | 3.08 | 0.88 |
| My teacher tells me I am good at math | 457 | 1.00 | 4.00 | 3.08 | 0.94 |
| Math is harder for me than other subjects (reverse coded) | 457 | 1.00 | 4.00 | 2.65 | 1.19 |
| My family thinks I am good at math | 457 | 1.00 | 4.00 | 3.25 | 0.88 |
| Value Scale Average | 457 | 1.33 | 4.00 | 3.28 | 0.54 |
| It is important to do well in math | 457 | 2.00 | 4.00 | 3.84 | 0.40 |
| Learning math will help me in daily life | 457 | 1.00 | 4.00 | 3.40 | 0.80 |
| I need math to learn other subjects | 457 | 1.00 | 4.00 | 3.26 | 0.79 |
| I need to do well in math to get into college | 457 | 1.00 | 4.00 | 3.54 | 0.75 |
| I need to do well in math to get the job I want | 457 | 1.00 | 4.00 | 3.29 | 0.89 |
| I would like a job that uses math | 457 | 1.00 | 4.00 | 2.34 | 1.07 |
| Like Learning Scale Average | 457 | 1.00 | 4.00 | 2.89 | 0.67 |
| I enjoy learning math | 457 | 1.00 | 4.00 | 3.10 | 0.84 |
| I wish I did not have to study math (reverse coded) | 457 | 1.00 | 4.00 | 2.84 | 1.01 |
| Math is boring (reverse coded) | 457 | 1.00 | 4.00 | 2.68 | 0.96 |
| I learn interesting things in math | 457 | 1.00 | 4.00 | 3.34 | 0.83 |
| I like math | 456 | 1.00 | 4.00 | 2.94 | 1.02 |
| I think of things not related to the lesson (reverse coded) | 457 | 1.00 | 4.00 | 2.21 | 0.84 |
| I am interested in what my math teacher says | 457 | 1.00 | 4.00 | 3.06 | 0.85 |
| My math teacher gives me interesting things to do | 457 | 1.00 | 4.00 | 2.92 | 0.97 |

Note. All negative items above were reverse coded (e.g., Math is boring) so that on all items higher scores mean more positive student ratings. Also, 1 student did not feel he could answer "I like math".

Student Ratings for Math Subscales by Year

|  | $6^{\text {th }}$ Grade |  | $7^{\text {th }}$ Grade |  | $8^{\text {th }}$ Grade |  | 9th Grade |  | $10^{\text {th }}$ Grade |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MEAN | SD | MEAN | SD | MEAN | SD | MEAN | SD | MEAN | SD |
| Students' Confidence in Mathematics Avg | 3.22 | 0.58 | 3.07 | 0.62 | 3.01 | 0.65 | 2.94 | 0.69 | 2.92 | 0.67 |
| Students Value Mathematics Avg | 3.55 | 0.40 | 3.52 | 0.42 | 3.47 | 0.43 | 3.39 | 0.50 | 3.28 | 0.54 |
| Students Like Learning Mathematics Avg | 3.37 | 0.53 | 3.21 | 0.60 | 3.06 | 0.62 | 2.98 | 0.67 | 2.89 | 0.67 |

## Student Survey Outcomes: TIMSS Science

|  | $\mathbf{N}$ | Min | Max | Mean | SD |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Confidence Scale Average | $\mathbf{4 5 7}$ | $\mathbf{1 . 2 5}$ | $\mathbf{4 . 0 0}$ | $\mathbf{2 . 9 9}$ | $\mathbf{0 . 6 3}$ |
| I know what my science teacher expects | 457 | 1.00 | 4.00 | 3.46 | 0.73 |
| My science teacher is easy to understand | 457 | 1.00 | 4.00 | 2.93 | 0.98 |
| I usually do well in science <br> Science is more difficult for me than my classmates <br> (reverse coded) | 457 | 1.00 | 4.00 | 3.21 | 0.79 |
| Science is not one of my strengths (reverse coded) <br> I learn quickly in science | 457 | 1.00 | 4.00 | 3.00 | 0.94 |
| Science makes me confused and nervous (reverse <br> $\quad$ coded) | 457 | 1.00 | 4.00 | 2.72 | 1.03 |
| I am good at working out hard science problems <br> My teacher thinks I can do well in science class with | 457 | 1.00 | 4.00 | 2.95 | 0.96 |
| $\quad$ difficult materials | 457 | 1.00 | 4.00 | 2.54 | 0.96 |
| My teacher tells me I am good at science | 456 | 1.00 | 4.00 | 3.17 | 0.83 |
| Science is harder for me than other subjects |  |  | 4.00 | 2.99 | 0.94 |
| $\quad$ (reverse coded) | 457 | 1.00 | 4.00 | 3.07 | 0.98 |
| My family thinks I am good at science | 457 | 1.00 | 4.00 | 3.05 | 0.91 |
| Value Scale Average | 457 | $\mathbf{1 . 0 0}$ | $\mathbf{4 . 0 0}$ | $\mathbf{2 . 7 6}$ | $\mathbf{0 . 7 3}$ |
| It is important to do well in science | 457 | 1.00 | 4.00 | 3.37 | 0.73 |
| Learning science will help me in daily life | 457 | 1.00 | 4.00 | 2.82 | 0.97 |
| I need science to learn other subjects | 457 | 1.00 | 4.00 | 2.47 | 0.98 |
| I need to do well in science to get into college | 457 | 1.00 | 4.00 | 3.05 | 1.02 |
| I need to do well in science to get the job I want | 457 | 1.00 | 4.00 | 2.60 | 1.13 |
| I would like a job that uses science | 457 | 1.00 | 4.00 | 2.25 | 1.13 |
| Like Learning Scale Average | $\mathbf{4 5 7}$ | $\mathbf{1 . 0 0}$ | $\mathbf{4 . 0 0}$ | $\mathbf{2 . 8 3}$ | $\mathbf{0 . 6 7}$ |
| I enjoy learning science | 457 | 1.00 | 4.00 | 3.00 | 0.95 |
| I wish I did not have to study science (reverse |  |  |  | 2.86 | 1.02 |
| coded) | 457 | 1.00 | 4.00 | 2.86 | 0.87 |
| I read about science in my spare time | 457 | 1.00 | 4.00 | 1.69 | 0.97 |
| Science is boring (reverse coded) | 457 | 1.00 | 4.00 | 2.88 | 0.78 |
| I learn interesting things in science | 457 | 1.00 | 4.00 | 3.48 | 0.99 |
| I like science |  |  |  |  |  |
| I think of things not related to the lesson (reverse | 457 | 1.00 | 4.00 | 3.00 | 0.95 |
| $\quad$ coded) | 457 | 1.00 | 4.00 | 2.34 | 0.88 |
| I am interested in what my science teacher says | 457 | 1.00 | 4.00 | 3.06 | 0.90 |
| My science teacher gives me interesting things to do | 457 | 1.00 | 4.00 | 3.11 |  |

Note. All negative items above were reverse coded so that higher scores mean more positive ratings. Also, 1 student did not feel she could answer "My teacher tells me I am good at science".

## Student TIMSS Ratings by School Type

|  | CHARTER |  | HIGH |  | OTHER |  | PRIVATE |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | N | Mean | N | Mean | N | Mean | N | Mean |
| TIMSS Math: Confidence | 63 | 3.01 | 365 | 2.90 | 24 | 3.05 | 5 | 2.90 |
| TIMSS Math: Value | 63 | 3.27 | 365 | 3.28 | 24 | 3.26 | 5 | 3.23 |
| TIMSS Math: Liking | 63 | 2.93 | 365 | 2.87 | 24 | 3.02 | 5 | 2.88 |
| TIMSS Math: Total | 63 | 79.17 | 365 | 77.45 | 24 | 80.29 | 5 | 77.20 |
| TIMSS Science: Confidence | 63 | 2.93 | 365 | 3.00 | 24 | 2.92 | 5 | 3.18 |
| TIMSS Science: Value | 63 | 2.77 | 365 | 2.73 | 24 | 3.03 | 5 | 3.27 |
| TIMSS Science: Liking | 63 | 2.85 | 365 | 2.82 | 24 | 2.85 | 5 | 3.04 |
| TIMSS Science: Total | 63 | 77.44 | 365 | 77.80 | 24 | 78.83 | 5 | 85.20 |

## Teacher Survey

- The online teacher survey was changed in 2018-19. Teachers no longer reported on each individual child. Instead the focus of the instrument was on teacher practices. This year's survey was taken from the Surveys of Enacted Curriculum (Grades K-12 Mathematics) and C-SAIL Teacher Survey (K-12 Mathematics).
- This year's teacher survey included 3 major sections:
o Teacher background questions (demographics, education, experience)
o Class description questions (characteristics of target math class)
o Math content questions (math concepts covered in target math class and cognitive demand emphasis for each)
- We sent out 159 teacher surveys to teachers who had at least 1 participating student enrolled in their math class.
- For Grade 10, we have survey data on 127 teachers: 119 teachers ( $74.8 \%$ of the teacher sample) fully completed their surveys, and $\mathbf{8}$ teachers ( $5.0 \%$ ) completed part of the survey. We included all possible collected data in our analyses except for the following:
o We dropped all survey data for 1 teacher because he misunderstood the survey directions, and his data were unusable. Thus, the highest possible responses for any item will be 126.
0 We also dropped items related to student gender, student race/ethnicity, and student EL status data for 5 teachers who misunderstood how we wanted them to report these data. The rest of these teachers' survey data are included in the analyses.


## Section 1: Teacher Background

- Gender
o Female: 76 (60.3\%)
o Male: 50 (39.7\%)
- Ethnicity
o Asian or Pacific Islander: 3 (2.4\%)
o Black: 26 (20.6\%)
o Hispanic: 2 (1.6\%)
o White: 88 (69.8\%)
o American Indian or Alaska Native: 1 (0.8\%)
o Other: 3 (2.4\%)
o Prefer not to answer: 3 (2.4\%)
- Experience
o Years as a teacher
- This is $1^{\text {st }}$ year: 7 (5.6\%)
- 2-4 years: 32 (25.4\%)
- 5-10 years: 41 (32.5\%)
- More than 10 years: 46 (36.5\%)
o Years at current school
- This is $1^{\text {st }}$ year: 29 (23.0\%)
- 2-4 years: 56 (44.4\%)
- 5-10 years: 32 (25.4\%)
- More than 10 years: 9 (7.1\%)
- Licensure (categories add up to more than 100\%)
o Elementary license (at least): 8 (6.3\%)
o Middle Grades license (at least): 6 (4.8\%)
o Mathematics license (at least):
- Mathematics (6-12): 35 (27.8\%)
- Mathematics (7-12): 93 (73.8\%)
- Middle Grades Math (6-8): 18 (14.3\%)
o Special Education license (at least): 14 (11.1\%)
o Other license (at least): 11 (8.7\%)
- Education
o Highest degree earned
- Bachelor's degree: 46 (36.5\%)
- Master's degree: 55 (43.7\%)
- Master's degree + 30: 21 (16.7\%)
- Doctoral degree: 4 (3.2\%)
o Majored in math in undergraduate program
- Yes: 73 (57.9\%)
- No: 53 (42.1\%)
o Minored in math in undergraduate program
- Yes: 10 (7.9\%)
- No: 89 (70.6\%)
- No minor (N/A): 27 (21.4\%)
o Majored in math in graduate school
- Yes: 23 (18.3\%)
- No: 72 (57.1\%)
- No grad school (N/A): 31 (24.6\%)
o Ever majored or minored in math
- Yes: 88 (69.8\%)
- No: 38 (30.2\%)


## Section 2: Description of Target Math Class

In this section, teachers were shown a list of all of the participating students enrolled in their math classes. Then, they were asked to select a target math class by choosing the math period/block they taught which contained the largest number of our study participants.

The target math class was used as a reference for filling out the remaining portions of the survey, which included questions about the composition of the target math class (section 2 ), and questions about the math content covered in the target math class (section 3).

- Name of Target Math Period/Block
o Integrated Math I: 24 (19.0\%)
o Integrated Math II: 48 (38.1\%)
o Integrated Math III: 17 (13.5\%)
o Algebra: 11 (8.7\%)
o Geometry: 20 (15.9\%)
o Trigonometry: 1 (0.8\%)
o Advanced Math: 3 (2.4\%)
o Other: 2 (1.6\%)
Name of Target Math Class by School Type

|  | School Type |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Name of Target Math Class | High School | Charter | Private | Other |
| Advanced Math | 3 | 0 | 0 | 0 |
| Algebra | 5 | 3 | 3 | 0 |
| Geometry | 18 | 2 | 0 | 0 |
| Integrated Math I | 19 | 2 | 0 | 3 |
| Integrated Math II | 39 | 5 | 0 | 4 |
| Integrated Math III | 13 | 1 | 0 | 3 |
| Other | 2 | 0 | 0 | 0 |
| Trigonometry | 1 | 0 | 0 | 0 |
| TOTAL | $\mathbf{1 0 0}$ | $\mathbf{1 3}$ | $\mathbf{3}$ | $\mathbf{1 0}$ |

- Grade Level of Most Students in Target Class

| 0 | $9^{\text {th }}: 29(23.0 \%)$ |
| :--- | :--- |
| 0 | $10^{\text {th }}: 86(68.3 \%)$ |
| 0 | $11^{\text {th }}: 9(7.1 \%)$ |
| 0 | $12^{\text {th }}: 2(1.6 \%)$ |

- Total \# of Students in Target Class

| $\mathbf{N}$ | Min | Max | Mean | SD |
| :---: | :---: | :---: | :---: | :---: |
| 121 | 10 | 37 | 24 | 5.98 |

Note. We dropped data for five teachers on this item, as well as the ethnicity, gender, and EL items following. These teachers misunderstood the question and either only reported data for the study participants enrolled in their math classes $(\mathrm{N}=4)$ or reported data for all 94 students enrolled in their Integrated Math II courses ( $\mathrm{N}=1$ ).

- Proportion of Students in Target Math Class by Ethnicity

|  | $\mathbf{N}$ | Min | Max | Mean | SD |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Proportion of Students in Class who are Asian or <br> Pacific Islander | 121 | 0.00 | 0.29 | 0.03 | 0.56 |
| Proportion of Students in Class who are Hispanic | 121 | 0.00 | 0.88 | 0.17 | 0.18 |
| Proportion of Students in Class who are Black | 121 | 0.00 | 1.00 | 0.43 | 0.27 |
| Proportion of Students in Class who are White | 121 | 0.00 | 1.00 | 0.33 | 0.28 |
| Proportion of American Indian or Alaska Native <br> Students in Class | 121 | 0.00 | 0.05 | 0.00 | 0.01 |
| Proportion of Students in Class who are of Other Race | 121 | 0.00 | 0.37 | 0.03 | 0.07 |

Note. Mean class size is 24 students. We dropped data for 5 teachers because they misunderstood the question about reporting ethnicity of students in the target math class.

Racial/Ethnic Majority of Students in Target Math Class

|  | All Study Schools |  | Public Schools in Davidson <br> County |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Freq | Pct | Freq | Pct |
| Majority White | 30 | 24.8 | 7 | 8.5 |
| Majority Black | 42 | 34.7 | 38 | 46.3 |
| Majority Hispanic | 8 | 6.6 | 8 | 9.8 |
| No Racial/Ethnic Majority | 41 | 33.9 | 29 | 35.4 |

Note. A class was defined as majority white if at least $51 \%$ of students were white, majority black if at least $51 \%$ of students were black, etc. We dropped data for 5 teachers because they misunderstood how we wanted them to report ethnicity data on their students.
\# Classes of Each Type by Racial Composition of Students in Target Math Class

|  | Majority Race/Ethnic Group |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Name of Target Math Class | Majority <br> White | Majority <br> Black | Majority <br> Hispanic | No <br> Majority | TOTAL |
| Integrated Math I | 3 | 9 | 2 | 9 | $\mathbf{2 3}$ |
| Integrated Math II | 5 | 19 | 4 | 18 | $\mathbf{4 6}$ |
| Integrated Math III | 3 | 6 | 0 | 7 | $\mathbf{1 6}$ |
| Algebra | 4 | 3 | 1 | 2 | $\mathbf{1 0}$ |
| Geometry | 12 | 4 | 1 | 3 | $\mathbf{2 0}$ |
| Advanced Math | 2 | 0 | 0 | 1 | $\mathbf{3}$ |
| Trigonometry | 1 | 0 | 0 | 0 | $\mathbf{1}$ |
| Other | 0 | 1 | 0 | 1 | $\mathbf{2}$ |
| TOTAL | $\mathbf{3 0}$ | $\mathbf{4 2}$ | $\mathbf{8}$ | $\mathbf{4 1}$ |  |

Note. We dropped data for 5 teachers because they misunderstood how we wanted them to report ethnicity data on their students.

- Gender of Students in Target Class

| Student Gender | Min. \# Students <br> in Class | Max. \# Students <br> in Class | Avg. \# Students <br> in Class |
| :--- | :---: | :---: | :---: |
| Male | 3 | 27 | 12 |
| Female | 1 | 24 | 12 |

Note. We dropped data for 5 teachers because they misunderstood how we wanted them to report gender data on their students.

- English Learner (EL) Status of Students in Target Class

| EL Status | Min. \# Students <br> in Class | Max. \# Students <br> in Class | Avg. \# Students <br> in Class |
| :--- | :---: | :---: | :---: |
| English Learner | 0 | 30 | 2 |
| Not English Learner | 0 | 36 | 22 |

Note. We dropped data for 5 teachers because they misunderstood how we wanted them to report EL data on their students.

- Number of Instructional Hours Target Class Spends in Math Instruction Per Week
o 2 hours: 1 (0.8\%)
o 3 hours: 34 (27.0\%)
o 4 hours: 34 (27.0\%)
o 5 hours: 27 (21.4\%)
o 6 hours: 5 (4.0\%)
o 7 hours: 19 (15.1\%)
o 8 hours: 3 (2.4\%)
o 9 hours: 1 (0.8\%)
Note. Two teachers (1.6\% of completed surveys) accidentally left this item blank.
- Average Length of Each Class Period for Target Math Class
o 41 to 50 minutes: 21 (16.7\%)
o 51 to 60 minutes: 15 (11.9\%)
o 61 to 90 minutes: 83 (65.9\%)
o 91 to 120 minutes: 3 (2.4\%)
o Varies Due to Block Scheduling: 4 (3.2\%)
- Total \# of Weeks the Target Math Class Will Meet This Year
o 1 to 12: 2 (1.6\%)
o 13 to 24: 12 (9.5\%)
o 25 or More: 112 (88.9\%)
- Achievement Level of Most Students in Target Class Compared to National Norms
o High Achievement Levels: 15 (11.9\%)
o Average Achievement Levels: 21 (16.7\%)
o Low Achievement Levels: 48 (38.1\%)
o Mixed Achievement Levels: 42 (33.3\%)
Teachers' Ratings of Math Achievement Level in Target Math Class by Course Name

|  | Math Achievement Level |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Name of Target Math Class | High | Average | Low | Mixed |
| Integrated Math I | 1 | 1 | 15 | 7 |
| Integrated Math II | 6 | 7 | 16 | 19 |
| Integrated Math III | 6 | 4 | 3 | 4 |
| Algebra | 1 | 2 | 5 | 3 |
| Geometry | 1 | 7 | 8 | 4 |
| Advanced Math | 0 | 0 | 0 | 3 |
| Trigonometry | 0 | 0 | 0 | 1 |
| Other | 0 | 0 | 1 | 1 |
| TOTAL | $\mathbf{1 5}$ | $\mathbf{2 1}$ | $\mathbf{4 8}$ | $\mathbf{4 2}$ |

- What is Considered Most When Scheduling Students into Target Class
o Ability or Prior Achievement: 45 (35.7\%)
o Limited English Proficiency: 4 (3.2\%)
o Teacher Recommendation: 1 (0.8\%)
o IEP Recommendation: 11 (8.7\%)
o Parent Request: 2 (1.6\%)
o Student Decision: 6 (4.8\%)
o No One Factor More Than Another: 57 (45.2\%)


## Section 3: Content Covered in Target Math Class

> Level of Coverage:
> $0=$ none
> $1=$ less than 1 class lesson
> $2=1$ to 5 class lessons
> $3=$ more than 5 lessons

Cognitive Demand Emphasis
$0=$ no focus
1 = minor focus
2 = moderate focus
3 = major focus
Note. For each topic, only one value of 3 (major focus) may be selected.

Average Level of Coverage \& Cognitive Demand Emphasis by Math Domain for All Teachers who Completed a Survey

|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recall/Perform Procedures |  |  |  |  | Demonstrate/Communicate Understanding |  |  |  |  | Generalize |  |  |  |  |
| Math Domain | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| Number Properties \& Operations | 123 | 0.0 | 3.0 | 1.78 | 0.76 | 122 | 0.5 | 3.0 | 1.82 | 0.54 | 122 | 0.5 | 3.0 | 1.72 | 0.52 | 122 | 0.0 | 3.0 | 1.48 | 0.71 |
| Basic Algebra | 123 | 0.0 | 3.0 | 1.85 | 0.63 | 121 | 1.0 | 3.0 | 1.95 | 0.44 | 121 | 0.57 | 3.0 | 1.90 | 0.47 | 121 | 0.0 | 3.0 | 1.62 | 0.62 |
| Advanced Algebra | 122 | 0.0 | 3.0 | 0.95 | 0.55 | 115 | 0.50 | 3.0 | 1.97 | 0.52 | 115 | 0.63 | 2.75 | 1.79 | 0.50 | 115 | 0.0 | 3.0 | 1.39 | 0.72 |
| Functions | 122 | 0.0 | 2.92 | 1.19 | 0.64 | 116 | 0.57 | 3.0 | 1.90 | 0.53 | 116 | 0.25 | 3.0 | 1.89 | 0.53 | 116 | 0.0 | 3.0 | 1.53 | 0.67 |
| Geometric Concepts | 122 | 0.0 | 2.78 | 0.94 | 0.62 | 118 | 1.0 | 3.0 | 1.92 | 0.52 | 118 | 0.0 | 3.0 | 1.87 | 0.54 | 118 | 0.0 | 3.0 | 1.36 | 0.68 |
| Trigonometry | 121 | 0.0 | 3.0 | 0.89 | 0.74 | 94 | 1.0 | 3.0 | 2.04 | 0.63 | 94 | 0.0 | 3.0 | 1.90 | 0.61 | 94 | 0.0 | 3.0 | 1.49 | 0.75 |

## Average Level of Coverage by Type of Target Math Class

| Math Domain | Integrated Math I <br> $\mathbf{( N = 2 3 )}$ | Integrated Math II <br> $\mathbf{( N = 4 8 )}$ | Integrated Math III <br> $\mathbf{( N = 1 7 )}$ | Algebra <br> $\mathbf{( N = \mathbf { 1 1 } )}$ | Geometry <br> $\mathbf{( N ~ = ~ 1 9 )}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  <br> Operations | 2.04 | 1.78 | 1.75 | 1.94 |  |
| Basic Algebra | 1.85 | 2.03 | 1.89 | 1.46 |  |
| Advanced Algebra | 0.81 | 1.21 | 1.11 | 2.15 | 1.14 |
| Functions | 1.08 | 1.30 | 1.76 | 1.46 | 0.36 |
| Geometric Concepts | 0.81 | 0.91 | 0.84 | 0.15 | 0.46 |
| Trigonometry | 0.24 | 1.13 | 0.86 | 1.89 |  |

Note. 1 IM II teacher only completed the "Number Properties \& Operations" and "Basic Algebra" sections of the survey, and 1 Geometry teacher accidentally skipped the Trigonometry section.

Average Cognitive Demand Emphasis by Type of Target Math Class

|  | Integrated Math I |  | Integrated Math II |  |  | Integrated Math III |  |  | Algebra |  |  | Geometry |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Math Domain | Recall <br> Avg. | Dem. <br> Avg. | Gen. <br> Avg. | Recall <br> Avg. | Dem. <br> Avg. | Gen. <br> Avg. | Recall <br> Avg. | Dem. <br> Avg. | Gen. <br> Avg. | Recall <br> Avg. | Dem. <br> Avg. | Gen. <br> Avg. | Recall <br> Avg. | Dem. <br> Avg. | Gen. <br> Avg. |
| Number Properties <br> \& Operations | 1.86 | 1.70 | 1.68 | 1.81 | 1.75 | 1.53 | 1.96 | 1.81 | 1.44 | 1.68 | 1.62 | 1.26 | 1.80 | 1.63 | 1.16 |
| Basic Algebra | 2.03 | 1.94 | 1.84 | 1.89 | 1.93 | 1.64 | 1.88 | 1.96 | 1.58 | 2.00 | 2.20 | 1.64 | 2.08 | 1.61 | 1.30 |
| Advanced Algebra | 1.94 | 1.70 | 1.57 | 2.07 | 1.91 | 1.47 | 1.84 | 1.90 | 1.46 | 1.95 | 1.76 | 1.19 | 1.90 | 1.47 | 0.92 |
| Functions | 1.92 | 1.76 | 1.66 | 1.82 | 1.90 | 1.56 | 2.01 | 2.08 | 1.56 | 1.76 | 2.04 | 1.49 | 2.21 | 1.52 | 1.15 |
| Geometric <br> Concepts | 1.92 | 1.70 | 1.29 | 1.84 | 1.90 | 1.38 | 1.94 | 2.07 | 1.44 | 1.79 | 1.49 | 1.14 | 2.29 | 1.98 | 1.35 |
| Trigonometry | 1.88 | 1.50 | 1.75 | 2.11 | 1.92 | 1.56 | 1.86 | 2.15 | 1.38 | 1.88 | 1.63 | 1.13 | 2.21 | 1.86 | 1.34 |

Average Level of Coverage in Integrated Math II Classes by Achievement Level of Target Math Class

|  | Achievement Level of Target Math Class |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | High (N = 6) |  | Average (N = 7) |  | Low (N = 16) |  | Mixed (N=19) |  |  |
| Math Domain | Mean | SD | Mean | SD | Mean | SD | Mean | SD |  |
| Number Properties \& Operations | 1.81 | 1.05 | 1.75 | 0.86 | 1.85 | 0.59 | 1.72 | 0.60 |  |
| Basic Algebra | 2.18 | 0.51 | 2.25 | 0.42 | 2.05 | 0.43 | 1.89 | 0.48 |  |
| Advanced Algebra | 1.40 | 0.33 | 1.20 | 0.49 | 1.20 | 0.53 | 1.17 | 0.33 |  |
| Functions | 1.63 | 0.56 | 1.12 | 0.49 | 1.38 | 0.46 | 1.20 | 0.54 |  |
| Geometric Concepts | 1.30 | 0.47 | 0.78 | 0.42 | 0.90 | 0.49 | 0.83 | 0.37 |  |
| Trigonometry | 1.36 | 0.59 | 0.81 | 0.37 | 1.22 | 0.40 | 1.10 | 0.53 |  |

Note. 1 teacher in the "Mixed" category only completed the "Number Properties \& Operations" and "Basic Algebra" sections of the survey.

Average Cognitive Demand Emphasis in Integrated Math II Classes by Achievement Level of Target Math Class

|  | Achievement Level of Target Math Class |  |  |  |  | Achievement Level of Target Math Class |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Math Domain | High | Average | Low | Mixed | Math Domain | High | Average | Low | Mixed |
| Number Properties \& Operations | Mean | Mean | Mean | Mean | Functions | Mean | Mean | Mean | Mean |
| Recall/Perform Procedures | 2.25 | 1.78 | 1.65 | 1.82 | Recall/Perform Procedures | 1.99 | 1.60 | 1.86 | 1.81 |
| Demonstrate/Communicate Understanding | 1.75 | 1.97 | 1.65 | 1.76 | Demonstrate/Communicate Understanding | 2.13 | 1.90 | 1.81 | 1.91 |
| Generalize | 1.58 | 1.96 | 1.44 | 1.43 | Generalize | 1.72 | 1.99 | 1.49 | 1.42 |
| Basic Algebra | Mean | Mean | Mean | Mean | Geometric Concepts | Mean | Mean | Mean | Mean |
| Recall/Perform Procedures | 2.14 | 1.74 | 1.92 | 1.85 | Recall/Perform Procedures | 2.18 | 1.40 | 1.88 | 1.85 |
| Demonstrate/Communicate Understanding | 2.22 | 1.99 | 1.85 | 1.87 | Demonstrate/Communicate Understanding | 2.22 | 1.99 | 1.79 | 1.85 |
| Generalize | 1.67 | 2.11 | 1.63 | 1.46 | Generalize | 1.42 | 1.84 | 1.38 | 1.20 |
| Advanced Algebra | Mean | Mean | Mean | Mean | Trigonometry | Mean | Mean | Mean | Mean |
| Recall/Perform Procedures | 2.35 | 1.94 | 1.96 | 2.12 | Recall/Perform Procedures | 2.24 | 1.69 | 2.18 | 2.16 |
| Demonstrate/Communicate Understanding | 2.02 | 1.96 | 1.84 | 1.93 | Demonstrate/Communicate Understanding | 2.17 | 2.00 | 1.78 | 1.92 |
| Generalize | 1.68 | 2.09 | 1.41 | 1.22 | Generalize | 1.78 | 2.19 | 1.38 | 1.39 |

Average Level of Coverage by Racial/Ethnic Composition of Target Math Class

|  | Racial/Ethnic Majority in Target Math Class |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Majority White (N=28) |  | Majority Black (N = 41) | No Majority (N=41) |  |  |
| Math Domain | Mean | SD | Mean | SD | Mean | SD |
| Number Properties \& Operations | 1.55 | 0.84 | 1.93 | 0.67 | 1.80 | 0.80 |
| Basic Algebra | 1.77 | 0.74 | 1.91 | 0.56 | 1.85 | 0.63 |
| Advanced Algebra | 0.89 | 0.62 | 0.99 | 0.54 | 1.04 | 0.55 |
| Functions | 0.98 | 0.77 | 1.25 | 0.53 | 1.27 | 0.68 |
| Geometric Concepts | 1.12 | 0.83 | 0.93 | 0.59 | 0.93 | 0.50 |
| Trigonometry | 1.09 | 0.84 | 0.87 | 0.72 | 0.89 | 0.73 |

Note. 3 teachers indicated the racial composition of their target math class but did not complete the math content items ( 2 in the majority white category, and 1 in the majority black category). Majority Hispanic classrooms are not included in this table because there were so few ( $n=8$ ).

Average Cognitive Demand Emphasis by Racial/Ethnic Composition of Target Math Class

|  | Racial/Ethnic Composition of Target Math Class |  |  |  | Racial/Ethnic Composition of Target Math Class |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Math Domain | Majority White | Majority Black | No Majority | Math Domain | Majority White | Majority Black | No <br> Majority |
| Number Properties \& Operations | Mean | Mean | Mean | Functions | Mean | Mean | Mean |
| Recall/Perform Procedures | 1.83 | 1.79 | 1.92 | Recall/Perform Procedures | 1.73 | 1.89 | 1.96 |
| Demonstrate/Communicate Understanding | 1.66 | 1.67 | 1.87 | Demonstrate/Communicate Understanding | 1.73 | 1.86 | 1.95 |
| Generalize | 1.17 | 1.50 | 1.67 | Generalize | 1.19 | 1.59 | 1.68 |
| Basic Algebra | Mean | Mean | Mean | Geometric Concepts | Mean | Mean | Mean |
| Recall/Perform Procedures | 2.06 | 1.89 | 1.95 | Recall/Perform Procedures | 2.08 | 1.89 | 1.84 |
| Demonstrate/Communicate Understanding | 1.77 | 1.87 | 2.03 | Demonstrate/Communicate Understanding | 1.74 | 1.81 | 1.99 |
| Generalize | 1.39 | 1.62 | 1.77 | Generalize | 1.11 | 1.43 | 1.50 |
| Advanced Algebra | Mean | Mean | Mean | Trigonometry | Mean | Mean | Mean |
| Recall/Perform Procedures | 1.86 | 1.95 | 2.00 | Recall/Perform Procedures | 2.05 | 2.04 | 2.01 |
| Demonstrate/Communicate Understanding | 1.63 | 1.82 | 1.90 | Demonstrate/Communicate Understanding | 1.75 | 1.83 | 2.05 |
| Generalize | 1.10 | 1.39 | 1.59 | Generalize | 1.16 | 1.46 | 1.80 |

## Teacher Interviews 2018-2019

In addition to the teacher surveys (which teachers filled out online during the spring semester), we completed individual, in-person teacher interviews during the fall of 2018.

We restricted our teacher interview sample for this year to only include teachers who worked at regular public schools in Davidson County. (NOTE: This is different than the teacher survey sample. We asked all teachers who had at least one participating student enrolled in their math class this year to complete a teacher survey.)

Among 112 teachers who were asked for an interview, 93 (83.4\%) interviews were completed.

Copies of the teacher interview and the coding scheme can be found in the Measures section of the binder.

- This year, we interviewed teachers from different types of in-county schools.

| School Type | Freq | Pct |
| :--- | :---: | :---: |
| Charter | 13 | 14.0 |
| Regular Public | 71 | 76.3 |
| Other (magnet or alternative) | 9 | 9.7 |

- Teachers were asked which math course(s) they taught.

| Code | Freq | Pct |
| :--- | :---: | :---: |
| Integrated Math I | 33 | 35.5 |
| Integrated Math II | 45 | 48.4 |
| Integrated Math III | 24 | 25.8 |
| Algebra I or II | 4 | 4.3 |
| Geometry | 3 | 3.2 |
| Advanced Math | 17 | 18.3 |

Note. Codes are not mutually exclusive.

Prompted Codes about High Quality Math Classrooms

- Teachers were asked questions about the role of a high quality math teacher and what class discussion would look like in a high quality math class.

| Code | Freq | Pct |
| :--- | :---: | :---: |
| Role of Teacher | 2 | 2.2 |
| 4 More Knowledgeable Other | 44 | 47.3 |
| 3 Facilitator | 21 | 22.6 |
| 2 Monitor | 25 | 26.9 |
| 1 Deliverer of Knowledge | 1 | 1.1 |
| 0 Motivator | 2 | 2.2 |
| 4 Whole Class Conversation Not Dependent on Teacher | 28 | 30.1 |
| 3 Whole Class Conversation Dependent on Teacher | 66 | 60.2 |
| 2 Student-Student Discourse Only in Small Groups | 6 | 6.5 |
| 1 Traditional Lecturing | 1 | 1.1 |
| Dropped for interviewer error | 10 | 10.8 |
| Nature of Classroom Talk <br> 4 Talk Should Be Conceptually Oriented <br> 3 Talk Is Calculation Oriented or Generally Involves <br> Questions/Explanations <br> 2 Talk is about Math but no Content Specifics <br> Did not discuss or discussed only talks between student and <br> teacher <br> Data Dropped for Interviewer Error | 13 | 14.0 |

## Teachers were asked what they find are the typical reasons students sometimes

 don't learn math as expected.| Code | Freq | Pct |
| :---: | :---: | :---: |
| General Productivity of Response |  |  |
| Productive (within teacher's control) | 2 | 2.2 |
| Unproductive (outside of teacher's control) | 73 | 78.5 |
| Mixed (productive and unproductive) | 18 | 19.4 |
| Reasons for Student Difficulties |  |  |
| Gaps in Student Knowledge | 52 | 55.9 |
| Teachers Need to Use Different Strategies | 21 | 22.6 |
| Student Laziness or Lack of Motivation | 45 | 48.4 |
| Home Life Issues | 6 | 6.5 |
| School System Issues | 3 | 3.2 |
| Students Lack Confidence | 29 | 31.2 |
| Bad Behavior | 5 | 5.4 |
| Poor Curriculum | 4 | 4.3 |
| Students Move Frequently | 0 | 0.0 |
| Class Sizes Too Large | 2 | 2.2 |

Note. The specific reasons for student difficulties are not mutually exclusive codes.

- Teachers were asked how they address the reasons their students don't learn math as expected.

| Code | Freq | Pct |
| :---: | :---: | :---: |
| General Productivity of Response |  |  |
| Productive (maintains high cognitive demand) | 6 | 6.5 |
| Unproductive (lowers the cognitive demand) | 75 | 80.6 |
| Mixed (productive and unproductive) | 11 | 11.8 |
| Dropped for interviewer error | 1 | 1.1 |
| Productive Teacher Strategies to Support Struggling Students |  |  |
| Focus on how task was launched | 5 | 5.4 |
| Use differentiated instruction or tasks with multiple entry points | 8 | 8.6 |
| Focus on "mastery" norms of participation | 2 | 2.2 |
| Assign competence to students' mathematical contributions | 2 | 2.2 |
| Group students in ways to maximize participation | 3 | 3.2 |
| Unproductive Teacher Strategies to Support Struggling Students |  |  |
| Shorten problems/remove prompts to explain thinking | 8 | 8.6 |
| Walk students through the steps of solving a problem | 17 | 18.3 |
| Study hall, tutoring, etc. as extra practice opportunities for struggling students | 35 | 37.6 |
| Teacher does not assign a math-specific strategy | 54 | 58.1 |

Note. The specific strategy codes are not mutually exclusive.

- We asked teachers with which academy they aligned their math courses. Depending on the type of response, we coded them into the following categories:

| Code | Freq | Pct |
| :--- | :--- | :---: | :---: |
| Teacher able to provide career academy name(s) with which <br> they align their math courses | 31 | 33.3 |
| Teacher able to provide career academy name(s) with which <br> they align their math courses, but admit they only partially <br> implement alignment | 2 | 2.2 |
| Teacher able to provide career academy name(s) with which <br> they align their math courses, but admit they do not implement <br> alignment | 7 | 7.5 |
| Teacher aligns math courses with the school's Freshman <br> Academy (not career academy) | 14 | 15.1 |
| Teacher aligns math courses with the school's Exceptional <br> Education program (not career academy) | 1 | 1.1 |
| School does not use academy model |  |  |

## - We asked the 40 Career Academy teachers about the advantages and disadvantages of career academies.

| Code | Freq | Pct |
| :---: | :---: | :---: |
| Do students benefit from academies? |  |  |
| Yes | 24 | 60.0 |
| No | 3 | 7.5 |
| Mixed (teacher mentions both pros and cons) | 13 | 32.5 |
| Subcodes for advantages of the career academy experience |  |  |
| Gain real-world experiences and expertise | 16 | 40.0 |
| Allow collaboration between stakeholders to connect course content to related fields | 9 | 22.5 |
| Opportunity to reflect on future career choices and education | 21 | 52.5 |
| Able to explore different interests/opportunities | 10 | 25.0 |
| Allow students to feel a sense of community | 9 | 22.5 |
| Other | 2 | 5 |
| Subcodes for disadvantages of the career academy experience |  |  |
| Focus is on assessments, standard tests, grades | 1 | 2.5 |
| Limited choices within career academy pathways | 8 | 20.0 |
| Student would benefit if they were in the same academy within a course | 1 | 2.5 |
| Students treated differently based on different prestige of academies | 1 | 2.5 |
| Inability to determine career choices at this age | 3 | 7.5 |
| Lack of planning and training for teachers | 1 | 2.5 |

Note. Specific subcodes for this section are not mutually exclusive.

## - We asked the 40 Career Academy teachers about professional development or training for career academies.

| Code | Freq | Pct |
| :---: | :---: | :---: |
| Has the teacher had professional development/training to help adapt their math instruction to fit the career academy model? |  |  |
| Yes | 15 | 37.5 |
| No | 20 | 50.0 |
| Teacher received other relevant training (not specific to the career academy model) | 5 | 12.5 |
| We asked how satisfied teachers felt about the amount of training received. |  |  |
| Teacher talked only about positive attributes of the training | 7 | 17.5 |
| Teacher talked only about negative attributes of the training | 2 | 5.0 |
| Teacher talked about both positive and negative attributes of the training | 6 | 15.0 |
| Teacher received no direct career academy training | 25 | 62.5 |
| For the teachers who were not satisfied with the training they have received, we asked the reason(s). |  |  |
| Trainings need to be more content specific | 2 | 5.0 |
| Trainings do not provide enough information, need more training | 3 | 7.5 |
| Lack of alignment between the training and math standards/curriculum | 1 | 2.5 |
| Other reasons unsatisfied | 2 | 5.0 |
| N/A (Teacher was satisfied about the training/received no direct academy training) | 32 | 80.0 |

Note. Specific subcodes for this section are not mutually exclusive.
Code Freq Pct
If teachers did not receive any training, we asked what kind of training they thought would helpthem to adapt their math instruction to fit the career academy model.
Training not needed ..... 7 ..... 17.5
Uncertain ..... 3 ..... 7.5
No interest ..... 3 ..... 7.5
Other ..... 7 ..... 17.5
N/A (Teacher received PD/training) ..... 20 ..... 50.0

- We asked teachers about adapting their math courses to align with the career academies.

Is it your responsibility to make adaptations between your math curriculum and the academies?


Note. Specific subcodes for this section are not mutually exclusive. Percent indicates percent of all teachers.

## Appendix

## Additional Information about Student Outcomes

## Distributions of Scores Across Direct Child Assessments

Woodcock-Johnson: Quantitative Concepts Subscale Distributions


## CMAT Grade Equivalent Distributions





## Relationship between KeyMath and CMAT





## Student Outcomes by Retention Status

Student Outcomes on Woodcock-Johnson Subtests by Retention Status

|  | N | Min | Max | Mean | Median | SD |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Not Retained <br> Average Age =15.98 years, Average Grade $=10.75$ <br> Quantitative Concepts |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| W-Score | 379 | 458.00 | 560.00 | 518.43 | 518.00 | 14.81 |
| Standard Score | 379 | 32.00 | 121.00 | 86.18 | 85.00 | 13.13 |
|  | N | Min | Max | Mean | Median | SD |
| Retained Average Age = 15.87 years, Average Grade $=9.75$ Quantitative Concepts |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| W-Score | 77 | 477.00 | 538.00 | 505.43 | 505.00 | 11.97 |
| Standard Score | 77 | 49.00 | 105.00 | 74.87 | 75.00 | 10.78 |

Student Outcomes on CMAT by Retention Status

|  | N | Min | Max | Mean | Median | SD |
| :--- | :--- | :--- | :--- | ---: | ---: | ---: |
| Not Retained <br> Average Age =15.95 years, Average Grade <br> CMAT: Problem Solving | $\mathbf{1 0 . 7 5}$ |  |  |  |  |  |
| $\quad$ Age-Based Standard Score | 380 | 1.0 | 15.0 | 8.0 | 8.0 | 2.9 |
| $\quad$ Age Equivalent | 380 | 6.9 | 18.0 | 13.5 | 12.6 | 3.3 |
| $\quad$ Grade Equivalent | 380 | 1.7 | 12.7 | 8.3 | 7.4 | 3.2 |
| CMAT: Algebra |  |  |  |  |  |  |
| $\quad$ Age-Based Standard Score | 380 | 1.0 | 17.0 | 7.5 | 7.5 | 3.2 |
| $\quad$ Age Equivalent | 380 | 8.3 | 18.3 | 13.5 | 13.9 | 3.1 |
| $\quad$ Grade Equivalent | 380 | 3.2 | 12.7 | 8.3 | 8.7 | 3.0 |
| CMAT: Geometry |  |  |  |  |  |  |
| $\quad$ Age-Based Standard Score | 380 | 1.0 | 16.0 | 7.3 | 6.0 | 3.0 |
| Age Equivalent | 380 | 8.9 | 18.3 | 13.2 | 12.6 | 2.7 |
| Grade Equivalent | 380 | 3.7 | 12.7 | 8.0 | 7.4 | 2.5 |


|  | N | Min | Max | Mean | Median | SD |
| :--- | :---: | :---: | ---: | ---: | ---: | ---: |
| Retained <br> Average Age = 15.82 years, Average Grade | $\mathbf{9 . 7 5}$ |  |  |  |  |  |
| CMAT: Problem Solving |  |  |  |  |  |  |
| $\quad$ Age-Based Standard Score | 77 | 1.0 | 12.0 | 5.7 | 5.0 | 2.6 |
| $\quad$ Age Equivalent | 77 | 6.3 | 18.0 | 10.9 | 10.3 | 2.4 |
| $\quad$ Grade Equivalent | 77 | 1.2 | 12.7 | 5.7 | 5.2 | 2.4 |
| CMAT: Algebra |  |  |  |  |  |  |
| $\quad$ Age-Based Standard Score | 77 | 1.0 | 10.0 | 4.6 | 4.0 | 2.2 |
| Age Equivalent | 77 | 8.3 | 16.0 | 10.7 | 9.9 | 1.9 |
| $\quad$ Grade Equivalent | 77 | 3.2 | 11.0 | 5.6 | 4.7 | 1.9 |
| CMAT: Geometry |  |  |  |  |  |  |
| $\quad$ Age-Based Standard Score | 77 | 1.0 | 10.0 | 5.4 | 6.0 | 1.6 |
| Age Equivalent | 77 | 8.3 | 14.9 | 11.2 | 11.3 | 1.2 |
| Grade Equivalent | 77 | 3.2 | 9.7 | 6.1 | 6.2 | 1.2 |

## Low Performing Students

- Students were selected who were below an eighth-grade level this past year on all 3 CMAT subscales.
- This group ended up including 167 students, which is about $32 \%$ of the current sample.


## Comparison of Low and Not Low Scoring Students on $10^{\text {th }}$ Grade Assessments

| Descriptive Statistics |  |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | Low-Scoring |  |  |  | Not Low-Scoring |  |  |  |  |  |
|  | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| CMAT PS (Std. Score) | 167 | 1.00 | 9.00 | 5.26 | 2.12 | 290 | 1.00 | 15.00 | 9.02 | 2.53 |
| CMAT Alg. (Std. Score) | 167 | 1.00 | 6.00 | 3.90 | 1.61 | 290 | 1.00 | 17.00 | 8.77 | 2.54 |
| CMAT Geo. (Std. Score) | 167 | 1.00 | 8.00 | 5.27 | 1.41 | 290 | 2.00 | 16.00 | 8.02 | 3.03 |
| WJ Quant. Cpts. (Std. Score) | 167 | 40.00 | 105.00 | 73.98 | 9.69 | 289 | 32.00 | 121.00 | 90.22 | 11.59 |
| TIMSS Math (Total) | 167 | 35.00 | 103.00 | 73.37 | 13.99 | 290 | 36.00 | 104.00 | 80.40 | 13.69 |
| TIMSS Science (Total) | 167 | 39.00 | 106.00 | 77.81 | 14.83 | 290 | 33.00 | 107.00 | 77.93 | 14.97 |

Note. Due to assessor error, we dropped WJ Quant Concepts scores for 1 student.

## Characteristics of Low-Scoring Students

|  | Low-Scoring |  | Not Low-Scoring |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Freq | Pct | Freq | Pct |
| Ethnicity |  |  |  |  |
| Black | 148 | 40.9 | 214 | 59.1 |
| White | 9 | 26.5 | 25 | 73.5 |
| Hispanic | 9 | 22.0 | 32 | 78.0 |
| Other | 1 | 5.0 | 19 | 95.0 |
| Gender | 71 | 36.0 | 126 | 64.0 |
| Male | 96 | 36.9 | 164 | 63.1 |
| Female | 157 | 81.8 | 35 | 18.2 |
| ELL in Pre-K Year | 10 | 3.8 | 254 | 96.2 |
| ELL |  |  |  |  |
| Not ELL | 96 | 34.2 | 185 | 65.8 |
| Pre-K Curriculum Condition | 71 | 40.3 | 105 | 59.7 |
| Building Blocks |  |  |  |  |
| Control | 70 | 38.3 | 113 | 61.7 |
| Pre-K School System | 97 | 35.4 | 177 | 64.6 |
| Head Start |  |  |  |  |
| MNPS Pre-K |  |  |  |  |


|  | Low-Scoring |  | Not Low-Scoring |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Freq | Pct | Freq | Pct |
| Grade 5 School Type |  |  |  |  |
| Charter | 21 | 22.1 | 74 | 77.9 |
| Izone | 31 | 45.6 | 37 | 54.4 |
| Middle | 71 | 30.5 | 162 | 69.5 |
| Other | 1 | 100.0 | 0 | 0.0 |
| Elementary | 43 | 71.7 | 17 | 28.3 |
| Grade 6 School Type |  |  |  |  |
| Charter | 29 | 26.4 | 81 | 73.6 |
| Izone | 29 | 46.0 | 34 | 54.0 |
| Middle | 107 | 38.2 | 173 | 61.8 |
| Other | 2 | 66.7 | 1 | 33.3 |
| Grade 7 School Type |  |  |  |  |
| Charter | 27 | 26.7 | 74 | 73.3 |
| Izone | 26 | 46.4 | 30 | 53.6 |
| Middle | 111 | 38.0 | 181 | 62.0 |
| Other | 1 | 50.0 | 1 | 50.0 |
| Private | 0 | 0.0 | 1 | 100.0 |
| Grade 8 School Type |  |  |  |  |
| Charter | 24 | 26.1 | 68 | 73.9 |
| Izone | 18 | 48.6 | 19 | 51.4 |
| Middle | 115 | 37.5 | 192 | 62.5 |
| Other | 7 | 43.8 | 9 | 56.3 |
| Private | 1 | 50.0 | 1 | 50.0 |
| Grade 9 School Type |  |  |  |  |
| Charter | 16 | 22.9 | 54 | 77.1 |
| Izone | 7 | 87.5 | 1 | 12.5 |
| Middle | 33 | 68.8 | 15 | 31.3 |
| High | 103 | 34.3 | 197 | 65.7 |
| Other | 6 | 24.0 | 19 | 76.0 |
| Private | 0 | 0.0 | 4 | 100.0 |
| Grade 10 School Type |  |  |  |  |
| Charter | 13 | 20.6 | 50 | 79.4 |
| High School | 146 | 40.0 | 219 | 60.0 |
| Private | 0 | 0.0 | 5 | 100.0 |
| Other | 8 | 33.3 | 16 | 66.7 |

Note. 1 student was out-of-region in Grade 6, 5 were out-of-region in Grade 7, 3 were out-of-region in Grade 8, and in Grade 9, 1 student was out-of-region and 1 student could not be located. Also, 1 student is missing a pre-k year ELL designation.

## Early Correlates of Later Skills

| Zero-Order Correlations: All Students |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} \text { Fall } \\ \text { PK QC } \\ \text { (Std } \\ \text { Score) } \end{gathered}$ | Spring <br> PK QC <br> (Std <br> Score) | $\begin{aligned} & \text { Spring } \\ & \text { K QC } \\ & \text { (Std } \\ & \text { Score) } \end{aligned}$ | Spring <br> G1 QC <br> (Std <br> Score) | $\begin{aligned} & \text { Fall } \\ & \text { PK AP } \\ & \text { (Std } \\ & \text { Score) } \end{aligned}$ | Spring <br> PK AP <br> (Std <br> Score) | $\begin{aligned} & \text { Spring } \\ & \text { K AP } \\ & \text { (Std } \\ & \text { Score) } \end{aligned}$ | Spring <br> G1 AP <br> (Std <br> Score) | Fall PK REMA NUM | Spring PK REMA NUM | $\begin{gathered} \text { Spring } \\ \text { K } \\ \text { REMA } \\ \text { NUM } \end{gathered}$ | Spring <br> G1 <br> REMA <br> NUM | $\begin{gathered} \text { Fall } \\ \text { PK } \\ \text { REMA } \\ \text { GEO } \end{gathered}$ | Spring PK REMA GEO | $\begin{gathered} \text { Spring } \\ \text { K } \\ \text { REMA } \\ \text { GEO } \end{gathered}$ | Spring <br> G1 <br> REMA <br> GEO |
| $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | WJ Quant. Cpts. (Std Score) | 0.41 | 0.52 | 0.53 | 0.56 | 0.32 | 0.46 | 0.51 | 0.55 | 0.36 | 0.48 | 0.57 | 0.59 | 0.28 | 0.42 | 0.42 | 0.37 |
|  | TIMSS Math (Total) | 0.06 | 0.06 | 0.11 | 0.19 | -0.01 | 0.03 | 0.16 | 0.15 | 0.07 | 0.09 | 0.12 | 0.14 | 0.06 | 0.06 | 0.14 | 0.08 |
|  | TIMSS Science (Total) | 0.00 | -0.02 | 0.04 | 0.06 | 0.00 | 0.06 | 0.01 | 0.04 | -0.02 | -0.01 | -0.02 | -0.02 | 0.00 | -0.02 | 0.01 | -0.04 |
|  | CMAT Problem Solving (Std Score) | 0.38 | 0.45 | 0.48 | 0.53 | 0.31 | 0.44 | 0.51 | 0.57 | 0.33 | 0.45 | 0.53 | 0.56 | 0.31 | 0.43 | 0.42 | 0.45 |
|  | CMAT Algebra (Std Score) | 0.36 | 0.42 | 0.43 | 0.46 | 0.24 | 0.38 | 0.42 | 0.48 | 0.33 | 0.45 | 0.48 | 0.50 | 0.27 | 0.37 | 0.40 | 0.35 |
|  | CMAT Geometry (Std Score) | 0.40 | 0.46 | 0.45 | 0.47 | 0.24 | 0.38 | 0.45 | 0.44 | 0.32 | 0.37 | 0.41 | 0.40 | 0.27 | 0.33 | 0.31 | 0.33 |

Note. Red cells indicate correlations > .20.

## Student Survey Outcomes: <br> TIMSS Math and TIMSS Science

Comparing Student Survey Subscales in Grade 10


## Student Interviews

Students were individually interviewed during spring assessments about their plans for the future and how likely they thought they were to major in or pursue a career in math or science.

## Information from the $\mathbf{4 5 7}$ completed student interviews

- After high school, what are you most likely to do? (NOTE: These codes were not mutually exclusive.)
o Continue in school: 381 (83.4\%)
o Get a job: 59 (12.9\%)
o Volunteer: 0 (0.0\%)
o Join the military: 19 (4.2\%)
o Not sure: 25 (5.5\%)
o Other: 24 (5.3\%)


Note. Students who do not plan to pursue post-secondary education were coded as N/A for this question.


Note. Students who do not plan to pursue post-secondary education were coded as N/A for this question.


## Parent Interview

- Out of the 519 students in the official original sample, we were able to conduct parent interviews with 79.2\% ( $\mathrm{N}=411$ ). These are the responses to additional questions not summarized in the main report.


## Helping with students' math homework

| Who helps student most often with math homework |  |  |
| :--- | :---: | :---: |
|  | Frequency | Percent |
| Female guardian | 158 | 38.5 |
| Male guardian | 20 | 4.9 |
| Grandparent | 7 | 1.7 |
| Older sibling | 26 | 6.3 |
| Partner of parent | 1 | 0.2 |
| Adult relative | 3 | 0.7 |
| Adult nonrelative | 1 | 0.2 |
| Teacher/Tutor | 1 | 0.2 |
| Multiple responses | 2 | 0.5 |
| No one | 191 | 46.6 |

Note. 1 parent did not answer this interview question.
How often respondent or other adult helps student with math homework in a typical week
FrequencyPercent
Never ..... 193 ..... 47.1
Less than once a week ..... 62 ..... 15.1
1 to 2 times a week ..... 91 ..... 22.2
3 to 4 times a week ..... 47 ..... 11.5
5 or more times a week ..... 17 ..... 4.1
Note. 1 parent did not answer this interview question.
Where outside the home the student receives additional help with math homework after schoolAfter school program at school
8 ..... 2.0
After school program outside of school
40 ..... 9.8
Teacher/aide at school
2 ..... 0.5
Paid private tutor program
2 ..... 0.5
Neighbor/adult non relative home
0 ..... 0.0
Grandparent/adult relative home
10 ..... 2.4
Other
5 ..... 1.2
Multiple responses
297 ..... 72.4
Not applicable
Note. Not applicable means that the student did not receive additional help with math homework after school in some place other than the home. 1 parent did not answer this interview question.

| How informed respondent is about student's math instruction |  |  |
| :--- | :---: | :---: |
|  | Frequency | Percent |
| Not informed | 51 | 12.4 |
| Slightly informed | 81 | 19.8 |
| Somewhat informed | 123 | 30.0 |
| Very informed | 125 | 30.5 |
| Extremely informed | 30 | 7.3 |

Note. 1 parent did not answer this interview question.

## Parents' evaluation of students' interest and performance (math)

## Student's interest in math

|  | Frequency | Percent |
| :--- | :---: | :---: |
| Not interested | 20 | 4.9 |
| Slightly interested | 71 | 17.3 |
| Somewhat interested | 161 | 39.3 |
| Very interested | 116 | 28.3 |
| Extremely interested | 42 | 10.2 |

Note. 1 parent did not answer this interview question.

| Student's performance in math |  |  |
| :--- | :---: | :---: |
|  | Frequency | Percent |
| Very much below average | 4 | 1.0 |
| Below average | 65 | 15.9 |
| Average | 219 | 53.4 |
| Above average | 93 | 22.7 |
| Very much above average | 29 | 7.1 |

Note. 1 parent did not answer this interview question.

## Respondent's beliefs and expectations (math)

## Respondent's beliefs about own math skills

| Respondent's beliefs about own math skills |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Was good at math in <br> high school |  | Good at math now |  | Knows enough about <br> math to help student |  |
|  | Frequency | Percent | Frequency | Percent | Frequency | Percent |
| Not true | 93 | 22.7 | 74 | 18.0 | 88 | 21.5 |
| Slightly true | 72 | 17.6 | 91 | 22.2 | 94 | 22.9 |
| True half the time | 49 | 12.0 | 68 | 16.6 | 80 | 19.5 |
| Mostly true | 86 | 21.0 | 103 | 25.1 | 78 | 19.0 |
| Completely true | 108 | 26.3 | 74 | 18.0 | 70 | 17.1 |
| Don't know | 2 | 0.5 | 0 | 0.0 | 0 | 0.0 |

[^1]| Respondent's expectations of child |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Expects child to get good grades in math |  | Believes child will perform well in math in future grades |  | Believes math plays an important role in child's future |  |
|  | Frequency | Percent | Frequency | Percent | Frequency | Percent |
| Not true | 1 | 0.2 | 4 | 1.0 | 1 | 0.2 |
| Slightly true | 17 | 4.1 | 30 | 7.3 | 15 | 3.7 |
| True half the time | 22 | 5.4 | 31 | 7.6 | 16 | 3.9 |
| Mostly true | 98 | 23.9 | 117 | 28.5 | 73 | 17.8 |
| Completely true | 271 | 66.1 | 227 | 55.4 | 304 | 74.1 |
| Don't know | 1 | 0.2 | 1 | 0.2 | 1 | 0.2 |

[^2]
## Helping with students' science homework

## Who helps student most often with science homework

|  | Frequency | Percent |
| :--- | :---: | :---: |
| Female guardian | 125 | 30.6 |
| Male guardian | 10 | 2.4 |
| Grandparent | 2 | 0.5 |
| Older sibling | 18 | 4.4 |
| Partner of parent | 0 | 0.0 |
| Adult relative | 2 | 0.5 |
| Adult nonrelative | 0 | 0.0 |
| Teacher/Tutor | 0 | 0.0 |
| Multiple responses | 2 | 0.5 |
| No one | 250 | 61.1 |

Note. 2 parents did not answer this question.

| How often respondent or other adult helps student with science <br> homework in a typical week |  |  |
| :--- | :---: | :---: |
|  | Frequency | Percent |
| Never | 253 | 61.9 |
| Less than once a week | 60 | 14.7 |
| 1 to 2 times a week | 74 | 18.1 |
| 3 to 4 times a week | 17 | 4.2 |
| 5 or more times a week | 5 | 1.2 |

[^3]
## Where outside the home the student receives additional help with science homework after school

| After school program at school | 25 | 6.1 |
| :--- | :---: | :---: |
| After school program outside of school | 7 | 1.7 |
| Teacher/aide at school | 23 | 5.6 |
| Paid private tutor program | 0 | 0.0 |
| Neighbor/adult non relative home | 0 | 0.0 |
| Grandparent/adult relative home | 2 | 0.5 |
| Other | 8 | 2.0 |
| Multiple responses | 0 | 0.0 |
| Not applicable | 344 | 84.1 |

Note. Not applicable means that the student does not receive additional help with science homework after school in some place other than the home. 2 parents did not answer this question.

| How informed respondent is about student's science instruction |  |  |
| :---: | :---: | :---: |
| Not informed | Frequency | Percent |
| Slightly informed | 65 | 15.9 |
| Somewhat informed | 101 | 24.7 |
| Very informed | 107 | 26.2 |
| Extremely informed | 103 | 25.2 |

Note. 2 parents did not answer this question.
Parents' evaluation of students' interest and performance (science)
Student's interest in science
Frequency Percent

Not interested
33
8.1

Slightly interested
98
24.0

Somewhat interested
134
32.8

Very interested 92
22.5

Extremely interested 52
12.7

Note. 2 parents did not answer this question.

| Student's performance in science |  |  |
| :--- | :---: | :---: |
|  | Frequency | Percent |
| Very much below average | 2 | 0.5 |
| Below average | 33 | 8.1 |
| Average | 227 | 55.5 |
| Above average | 117 | 28.6 |
| Very much above average | 30 | 7.3 |

[^4]| Respondent's beliefs about own science skills |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | Was good at science in <br> high school |  |  | Good at science now | Knows enough about <br> science to help student |
|  | Frequency | Percent | Frequency | Percent | Frequency | Percent

Note. 1 parent did not answer this question.

| Respondent's expectations of child |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Expects child to get <br> good grades in <br> science | Believes child will <br> perform well in science <br> in future grades | Believes science plays <br> an important role in <br> child's future |  |  |  |
|  | Frequency | Percent | Frequency | Percent | Frequency | Percent |
| Not true | 2 | 0.5 | 2 | 0.5 | 5 | 1.2 |
| Slightly true | 15 | 3.7 | 27 | 6.6 | 45 | 11.0 |
| True half the time | 34 | 8.3 | 22 | 5.4 | 35 | 8.5 |
| Mostly true | 102 | 24.9 | 123 | 30.0 | 112 | 27.3 |
| Completely true | 257 | 62.7 | 236 | 57.6 | 212 | 51.7 |
| Don't know | 0 | 0.0 | 0 | 0.0 | 1 | 0.2 |

Note. 1 parent did not answer this question.

## Teacher Survey

This section includes supplemental information about the teacher survey. The table below shows the average level of coverage and cognitive demand emphasis that teachers reported for every item on the math content portion of the survey. Information and data from the rest of the teacher survey can be found in the main report, beginning on page 25 .

Level of Coverage \& Cognitive Demand Emphasis by Individual Math Item

|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recall/Perform Procedures |  |  |  |  | Demonstrate/Communicate Understanding |  |  |  |  | Generalize |  |  |  |  |
| Number Properties \& Operations |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| OVERALL | 123 | 0.0 | 3.0 | 1.78 | 0.76 | 122 | 0.5 | 3.0 | 1.82 | 0.54 | 122 | 0.5 | 3.0 | 1.72 | 0.52 | 122 | 0.0 | 3.0 | 1.48 | 0.71 |
| Integers | 123 | 0.0 | 3.0 | 1.67 | 1.12 | 99 | 0.0 | 3.0 | 1.80 | 0.77 | 98 | 0.0 | 3.0 | 1.81 | 0.65 | 99 | 0.0 | 3.0 | 1.57 | 0.87 |
| Fractions, decimals, and percents | 123 | 0.0 | 3.0 | 1.63 | 1.03 | 104 | 0.0 | 3.0 | 1.80 | 0.73 | 104 | 0.0 | 3.0 | 1.71 | 0.75 | 104 | 0.0 | 3.0 | 1.46 | 0.86 |
| Real and/or rational numbers | 123 | 0.0 | 3.0 | 1.72 | 1.11 | 98 | 0.0 | 3.0 | 1.84 | 0.74 | 98 | 0.0 | 3.0 | 1.67 | 0.72 | 98 | 0.0 | 3.0 | 1.52 | 0.88 |
| Exponents and scientific notation | 123 | 0.0 | 3.0 | 1.86 | 0.92 | 109 | 0.0 | 3.0 | 1.78 | 0.71 | 109 | 0.0 | 3.0 | 1.80 | 0.74 | 109 | 0.0 | 3.0 | 1.53 | 0.85 |
| Factors, multiples, and divisibility | 123 | 0.0 | 3.0 | 1.95 | 1.00 | 108 | 0.0 | 3.0 | 1.87 | 0.79 | 108 | 0.0 | 3.0 | 1.77 | 0.65 | 108 | 0.0 | 3.0 | 1.47 | 0.86 |
| Opposites, reciprocals, and identities | 123 | 0.0 | 3.0 | 1.62 | 1.07 | 100 | 0.0 | 3.0 | 1.75 | 0.73 | 100 | 0.0 | 3.0 | 1.71 | 0.76 | 100 | 0.0 | 3.0 | 1.40 | 0.87 |
| Mathematical properties | 123 | 0.0 | 3.0 | 2.10 | 1.00 | 111 | 0.0 | 3.0 | 2.02 | 0.75 | 111 | 0.0 | 3.0 | 1.81 | 0.73 | 111 | 0.0 | 3.0 | 1.50 | 0.85 |
| Operations on fractions and decimals | 123 | 0.0 | 3.0 | 1.64 | 1.03 | 102 | 0.0 | 3.0 | 1.79 | 0.74 | 102 | 0.0 | 3.0 | 1.61 | 0.75 | 102 | 0.0 | 3.0 | 1.54 | 0.89 |


|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recall/Perform Procedures |  |  |  |  | Demonstrate/Communicate Understanding |  |  |  |  | Generalize |  |  |  |  |
| Ratio and proportion | 123 | 0.0 | 3.0 | 1.80 | 1.00 | 107 | 0.0 | 3.0 | 1.74 | 0.71 | 107 | 0.0 | 3.0 | 1.81 | 0.66 | 107 | 0.0 | 3.0 | 1.64 | 0.82 |
| Basic Algebra |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| OVERALL | 123 | 0.0 | 3.0 | 1.85 | 0.63 | 121 | 1.0 | 3.0 | 1.95 | 0.44 | 121 | 0.57 | 3.0 | 1.90 | 0.47 | 121 | 0.0 | 3.0 | 1.62 | 0.62 |
| Use of variables | 123 | 0.0 | 3.0 | 2.34 | 0.99 | 110 | 0.0 | 3.0 | 1.95 | 0.72 | 110 | 1.0 | 3.0 | 2.07 | 0.52 | 110 | 0.0 | 3.0 | 2.01 | 0.72 |
| Formulas, expressions, and equations | 123 | 0.0 | 3.0 | 2.62 | 0.75 | 116 | 1.0 | 3.0 | 2.09 | 0.63 | 116 | 1.0 | 3.0 | 2.15 | 0.53 | 116 | 0.0 | 3.0 | 1.86 | 0.77 |
| One-step equations | 123 | 0.0 | 3.0 | 1.68 | 1.09 | 102 | 0.0 | 3.0 | 1.95 | 0.84 | 102 | 0.0 | 3.0 | 1.77 | 0.74 | 102 | 0.0 | 3.0 | 1.61 | 0.89 |
| Coordinate planes | 123 | 0.0 | 3.0 | 2.14 | 1.00 | 111 | 0.0 | 3.0 | 1.90 | 0.73 | 110 | 0.0 | 3.0 | 2.00 | 0.70 | 110 | 0.0 | 3.0 | 1.71 | 0.85 |
| Arithmetic or geometric patterns | 123 | 0.0 | 3.0 | 1.56 | 1.20 | 86 | 1.0 | 3.0 | 1.78 | 0.66 | 86 | 0.0 | 3.0 | 1.92 | 0.77 | 86 | 0.0 | 3.0 | 1.70 | 0.87 |
| Multi-step equations | 123 | 0.0 | 3.0 | 2.28 | 0.91 | 114 | 0.0 | 3.0 | 2.08 | 0.71 | 114 | 1.0 | 3.0 | 2.04 | 0.61 | 114 | 0.0 | 3.0 | 1.67 | 0.83 |
| Inequalities | 123 | 0.0 | 3.0 | 1.50 | 1.15 | 87 | 0.0 | 3.0 | 1.80 | 0.68 | 87 | 0.0 | 3.0 | 1.87 | 0.73 | 88 | 0.0 | 3.0 | 1.73 | 0.85 |
| Linear and nonlinear relations | 123 | 0.0 | 3.0 | 2.15 | 1.05 | 107 | 0.0 | 3.0 | 1.83 | 0.68 | 107 | 0.0 | 3.0 | 1.99 | 0.75 | 108 | 0.0 | 3.0 | 1.77 | 0.84 |
| Functions | 123 | 0.0 | 3.0 | 2.20 | 1.03 | 106 | 0.0 | 3.0 | 1.86 | 0.65 | 106 | 0.0 | 3.0 | 2.04 | 0.65 | 107 | 0.0 | 3.0 | 1.82 | 0.80 |
| Operations on functions | 123 | 0.0 | 3.0 | 1.89 | 1.17 | 97 | 1.0 | 3.0 | 1.94 | 0.69 | 97 | 0.0 | 3.0 | 1.89 | 0.66 | 97 | 0.0 | 3.0 | 1.64 | 0.86 |
| Rate of change/slope | 123 | 0.0 | 3.0 | 2.07 | 0.95 | 111 | 0.0 | 3.0 | 1.90 | 0.67 | 111 | 0.0 | 3.0 | 1.96 | 0.67 | 111 | 0.0 | 3.0 | 1.80 | 0.88 |
| Polynomials | 123 | 0.0 | 3.0 | 1.91 | 1.19 | 96 | 0.0 | 3.0 | 2.01 | 0.72 | 96 | 0.0 | 3.0 | 1.98 | 0.73 | 96 | 0.0 | 3.0 | 1.58 | 0.85 |
| Operations on polynomials | 123 | 0.0 | 3.0 | 1.97 | 1.12 | 101 | 0.0 | 3.0 | 2.08 | 0.77 | 101 | 0.0 | 3.0 | 1.83 | 0.76 | 101 | 0.0 | 3.0 | 1.43 | 0.88 |
| Factoring polynomials | 123 | 0.0 | 3.0 | 1.93 | 1.25 | 94 | 0.0 | 3.0 | 2.13 | 0.74 | 94 | 0.0 | 3.0 | 1.94 | 0.73 | 94 | 0.0 | 3.0 | 1.51 | 0.85 |
| Operations on radicals | 123 | 0.0 | 3.0 | 1.44 | 1.17 | 83 | 0.0 | 3.0 | 1.94 | 0.76 | 83 | 0.0 | 3.0 | 1.64 | 0.82 | 83 | 0.0 | 3.0 | 1.14 | 0.86 |


|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recall/Perform Procedures |  |  |  |  | Demonstrate/Communicate Understanding |  |  |  |  | Generalize |  |  |  |  |
| Rational expressions | 123 | 0.0 | 3.0 | 1.39 | 1.25 | 75 | 1.0 | 3.0 | 1.92 | 0.67 | 75 | 0.0 | 3.0 | 1.84 | 0.74 | 75 | 0.0 | 3.0 | 1.37 | 0.91 |
| Completing the square | 123 | 0.0 | 3.0 | 0.98 | 1.16 | 59 | 0.0 | 3.0 | 1.97 | 0.83 | 59 | 0.0 | 3.0 | 1.63 | 0.83 | 58 | 0.0 | 3.0 | 1.16 | 0.89 |
| Quadratic formula | 123 | 0.0 | 3.0 | 1.46 | 1.21 | 81 | 0.0 | 3.0 | 2.12 | 0.83 | 81 | 0.0 | 3.0 | 1.74 | 0.82 | 81 | 0.0 | 3.0 | 1.33 | 0.82 |
| Functions to model data | 123 | 0.0 | 3.0 | 1.55 | 1.14 | 89 | 1.0 | 3.0 | 1.58 | 0.56 | 89 | 0.0 | 3.0 | 1.93 | 0.69 | 89 | 0.0 | 3.0 | 2.03 | 0.82 |
| Advanced Algebra |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| OVERALL | 122 | 0.0 | 3.0 | 0.95 | 0.55 | 115 | 0.50 | 3.0 | 1.97 | 0.52 | 115 | 0.63 | 2.75 | 1.79 | 0.50 | 115 | 0.0 | 3.0 | 1.39 | 0.72 |
| Computational algebra | 122 | 0.0 | 3.0 | 1.38 | 1.24 | 76 | 0.0 | 3.0 | 2.12 | 0.71 | 76 | 0.0 | 3.0 | 1.84 | 0.69 | 76 | 0.0 | 3.0 | 1.51 | 0.86 |
| Quadratic equations | 122 | 0.0 | 3.0 | 1.76 | 1.30 | 85 | 0.0 | 3.0 | 2.02 | 0.77 | 85 | 0.0 | 3.0 | 2.01 | 0.76 | 85 | 0.0 | 3.0 | 1.65 | 0.83 |
| Systems of equations | 122 | 0.0 | 3.0 | 1.48 | 1.13 | 87 | 0.0 | 3.0 | 1.86 | 0.77 | 87 | 0.0 | 3.0 | 1.72 | 0.79 | 87 | 0.0 | 3.0 | 1.60 | 0.97 |
| Systems of inequalities | 122 | 0.0 | 3.0 | 0.95 | 1.04 | 63 | 0.0 | 3.0 | 1.67 | 0.76 | 63 | 0.0 | 3.0 | 1.70 | 0.78 | 63 | 0.0 | 3.0 | 1.52 | 0.97 |
| Compound inequalities | 122 | 0.0 | 3.0 | 0.54 | 0.86 | 39 | 0.0 | 3.0 | 1.69 | 0.69 | 39 | 0.0 | 3.0 | 1.67 | 0.66 | 39 | 0.0 | 3.0 | 1.51 | 0.89 |
| Matrices and determinants | 122 | 0.0 | 3.0 | 0.20 | 0.62 | 14 | 1.0 | 3.0 | 1.93 | 0.83 | 14 | 1.0 | 2.0 | 1.64 | 0.50 | 14 | 0.0 | 3.0 | 1.43 | 1.02 |
| Conic sections | 122 | 0.0 | 3.0 | 0.24 | 0.66 | 17 | 1.0 | 3.0 | 1.71 | 0.77 | 17 | 1.0 | 3.0 | 1.71 | 0.59 | 17 | 0.0 | 3.0 | 1.24 | 0.75 |
| Rational, negative exponents, or radicals | 122 | 0.0 | 3.0 | 1.49 | 1.19 | 82 | 1.0 | 3.0 | 2.18 | 0.67 | 82 | 0.0 | 3.0 | 1.82 | 0.72 | 82 | 0.0 | 3.0 | 1.17 | 0.93 |
| Rules for exponents | 122 | 0.0 | 3.0 | 1.67 | 1.05 | 97 | 0.0 | 3.0 | 2.26 | 0.73 | 97 | 0.0 | 3.0 | 1.85 | 0.74 | 97 | 0.0 | 3.0 | 1.19 | 0.92 |
| Complex numbers | 122 | 0.0 | 3.0 | 1.03 | 1.16 | 59 | 1.0 | 3.0 | 2.10 | 0.74 | 59 | 0.0 | 3.0 | 1.86 | 0.71 | 59 | 0.0 | 3.0 | 1.14 | 0.94 |
| Binomial theorem | 122 | 0.0 | 3.0 | 0.21 | 0.71 | 11 | 1.0 | 3.0 | 1.73 | 0.79 | 11 | 1.0 | 3.0 | 1.91 | 0.70 | 11 | 0.0 | 3.0 | 1.91 | 0.94 |
| Factor/remainder theorem | 122 | 0.0 | 3.0 | 0.61 | 1.06 | 35 | 1.0 | 3.0 | 1.97 | 0.75 | 35 | 0.0 | 3.0 | 1.83 | 0.89 | 35 | 0.0 | 3.0 | 1.31 | 0.90 |


|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recall/Perform Procedures |  |  |  |  | Demonstrate/Communicate Understanding |  |  |  |  | Generalize |  |  |  |  |
| Field properties of real number system | 122 | 0.0 | 3.0 | 0.31 | 0.74 | 21 | 0.0 | 3.0 | 1.57 | 0.75 | 21 | 0.0 | 3.0 | 1.57 | 0.93 | 21 | 0.0 | 3.0 | 1.38 | 1.12 |
| Multiple representations | 122 | 0.0 | 3.0 | 1.47 | 1.27 | 77 | 0.0 | 3.0 | 1.68 | 0.62 | 77 | 0.0 | 3.0 | 2.06 | 0.71 | 77 | 0.0 | 3.0 | 1.95 | 0.86 |
| Functions |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| OVERALL | 122 | 0.0 | 2.92 | 1.19 | 0.64 | 116 | 0.57 | 3.0 | 1.90 | 0.53 | 116 | 0.25 | 3.0 | 1.89 | 0.53 | 116 | 0.0 | 3.0 | 1.53 | 0.67 |
| Notation | 122 | 0.0 | 3.0 | 1.40 | 1.13 | 84 | 0.0 | 3.0 | 1.90 | 0.75 | 84 | 0.0 | 3.0 | 1.89 | 0.78 | 84 | 0.0 | 3.0 | 1.40 | 0.92 |
| Relations | 122 | 0.0 | 3.0 | 1.17 | 1.10 | 75 | 0.0 | 3.0 | 1.63 | 0.67 | 75 | 0.0 | 3.0 | 1.88 | 0.81 | 75 | 0.0 | 3.0 | 1.52 | 0.89 |
| Linear | 122 | 0.0 | 3.0 | 1.76 | 1.11 | 98 | 1.0 | 3.0 | 1.89 | 0.67 | 98 | 0.0 | 3.0 | 1.88 | 0.68 | 98 | 0.0 | 3.0 | 1.79 | 0.90 |
| Quadratic | 122 | 0.0 | 3.0 | 1.75 | 1.28 | 88 | 1.0 | 3.0 | 1.99 | 0.69 | 88 | 0.0 | 3.0 | 2.05 | 0.73 | 88 | 0.0 | 3.0 | 1.66 | 0.86 |
| Polynomial | 122 | 0.0 | 3.0 | 1.48 | 1.31 | 76 | 0.0 | 3.0 | 1.92 | 0.71 | 76 | 0.0 | 3.0 | 1.93 | 0.72 | 76 | 0.0 | 3.0 | 1.46 | 0.87 |
| Rational | 122 | 0.0 | 3.0 | 0.95 | 1.23 | 51 | 1.0 | 3.0 | 1.88 | 0.62 | 51 | 0.0 | 3.0 | 1.90 | 0.73 | 51 | 0.0 | 3.0 | 1.51 | 0.86 |
| Logarithmic | 122 | 0.0 | 3.0 | 0.48 | 0.98 | 27 | 0.0 | 3.0 | 1.93 | 0.78 | 27 | 0.0 | 3.0 | 1.93 | 0.83 | 27 | 0.0 | 3.0 | 1.22 | 0.85 |
| Exponential | 122 | 0.0 | 3.0 | 1.74 | 1.17 | 92 | 0.0 | 3.0 | 1.82 | 0.65 | 92 | 0.0 | 3.0 | 1.91 | 0.66 | 92 | 0.0 | 3.0 | 1.86 | 0.91 |
| Trigonometric and circular | 122 | 0.0 | 3.0 | 0.89 | 1.19 | 50 | 1.0 | 3.0 | 2.08 | 0.75 | 50 | 0.0 | 3.0 | 1.78 | 0.71 | 50 | 0.0 | 3.0 | 1.46 | 0.86 |
| Inverse | 122 | 0.0 | 3.0 | 0.75 | 1.08 | 45 | 1.0 | 3.0 | 1.93 | 0.69 | 45 | 0.0 | 3.0 | 1.93 | 0.75 | 45 | 0.0 | 3.0 | 1.44 | 0.87 |
| Composition | 122 | 0.0 | 3.0 | 0.29 | 0.72 | 19 | 0.0 | 3.0 | 1.79 | 0.79 | 19 | 0.0 | 3.0 | 1.68 | 0.67 | 19 | 0.0 | 3.0 | 1.26 | 0.87 |
| Domain and range functions | 122 | 0.0 | 3.0 | 1.57 | 1.15 | 89 | 0.0 | 3.0 | 1.87 | 0.69 | 89 | 0.0 | 3.0 | 2.01 | 0.75 | 89 | 0.0 | 3.0 | 1.64 | 0.84 |
| Geometric Concepts |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| OVERALL | 122 | 0.0 | 2.78 | 0.94 | 0.62 | 118 | 1.0 | 3.0 | 1.92 | 0.52 | 118 | 0.0 | 3.0 | 1.87 | 0.54 | 118 | 0.0 | 3.0 | 1.36 | 0.68 |
| Basic terminology | 122 | 0.0 | 3.0 | 1.89 | 1.02 | 105 | 0.0 | 3.0 | 2.08 | 0.78 | 105 | 0.0 | 3.0 | 1.87 | 0.79 | 105 | 0.0 | 3.0 | 1.38 | 0.86 |
| Precise definitions of geometric objects and properties | 122 | 0.0 | 3.0 | 1.43 | 1.08 | 91 | 0.0 | 3.0 | 1.91 | 0.69 | 91 | 0.0 | 3.0 | 1.86 | 0.81 | 91 | 0.0 | 3.0 | 1.24 | 0.90 |
| Logic, reasoning, and proof | 122 | 0.0 | 3.0 | 1.28 | 1.22 | 71 | 0.0 | 3.0 | 1.76 | 0.67 | 71 | 0.0 | 3.0 | 2.08 | 0.79 | 71 | 0.0 | 3.0 | 1.41 | 0.94 |


|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recall/Perform Procedures |  |  |  |  | Demonstrate/Communicate Understanding |  |  |  |  | Generalize |  |  |  |  |
| Points, lines, rays, segments, and planes | 122 | 0.0 | 3.0 | 1.01 | 1.09 | 64 | 1.0 | 3.0 | 2.05 | 0.74 | 64 | 0.0 | 3.0 | 1.80 | 0.65 | 64 | 0.0 | 3.0 | 1.41 | 0.92 |
| Angles | 122 | 0.0 | 3.0 | 1.63 | 1.12 | 95 | 1.0 | 3.0 | 1.87 | 0.72 | 95 | 0.0 | 3.0 | 1.94 | 0.71 | 95 | 0.0 | 3.0 | 1.46 | 0.90 |
| Vectors | 122 | 0.0 | 2.0 | 0.25 | 0.57 | 22 | 0.0 | 3.0 | 1.82 | 0.96 | 22 | 0.0 | 3.0 | 1.45 | 0.91 | 22 | 0.0 | 3.0 | 0.95 | 0.90 |
| Rigid transformations | 122 | 0.0 | 3.0 | 1.57 | 1.25 | 82 | 0.0 | 3.0 | 1.95 | 0.77 | 82 | 0.0 | 3.0 | 1.99 | 0.76 | 82 | 0.0 | 3.0 | 1.44 | 0.94 |
| Dilations | 122 | 0.0 | 3.0 | 1.43 | 1.17 | 80 | 1.0 | 3.0 | 2.08 | 0.61 | 80 | 0.0 | 3.0 | 2.11 | 0.80 | 80 | 0.0 | 3.0 | 1.55 | 0.83 |
| Defining congruence in terms of transformations | 122 | 0.0 | 3.0 | 1.23 | 1.20 | 69 | 0.0 | 3.0 | 1.94 | 0.66 | 69 | 0.0 | 3.0 | 1.96 | 0.74 | 69 | 0.0 | 3.0 | 1.36 | 0.95 |
| Congruence of triangles | 121 | 0.0 | 3.0 | 1.31 | 1.27 | 69 | 0.0 | 3.0 | 1.93 | 0.73 | 69 | 0.0 | 3.0 | 2.03 | 0.80 | 69 | 0.0 | 3.0 | 1.39 | 0.93 |
| Congruence of other figures | 121 | 0.0 | 3.0 | 0.85 | 1.09 | 52 | 0.0 | 3.0 | 1.83 | 0.73 | 52 | 0.0 | 3.0 | 1.90 | 0.72 | 52 | 0.0 | 3.0 | 1.25 | 0.91 |
| Defining similarity in terms of transformations | 121 | 0.0 | 3.0 | 1.26 | 1.21 | 69 | 0.0 | 3.0 | 2.03 | 0.64 | 69 | 0.0 | 3.0 | 2.09 | 0.74 | 69 | 0.0 | 3.0 | 1.32 | 0.90 |
| Similarity of triangles | 121 | 0.0 | 3.0 | 1.52 | 1.28 | 76 | 1.0 | 3.0 | 2.03 | 0.69 | 76 | 0.0 | 3.0 | 2.09 | 0.72 | 76 | 0.0 | 3.0 | 1.49 | 0.90 |
| Similarity of other figures | 121 | 0.0 | 3.0 | 1.02 | 1.14 | 61 | 1.0 | 3.0 | 1.92 | 0.69 | 61 | 0.0 | 3.0 | 1.89 | 0.71 | 61 | 0.0 | 3.0 | 1.43 | 0.94 |
| Parallel lines | 121 | 0.0 | 3.0 | 1.31 | 1.12 | 79 | 1.0 | 3.0 | 1.94 | 0.74 | 79 | 0.0 | 3.0 | 1.78 | 0.80 | 79 | 0.0 | 3.0 | 1.37 | 0.96 |
| Classifying polygons | 121 | 0.0 | 3.0 | 0.92 | 1.12 | 56 | 1.0 | 3.0 | 2.09 | 0.70 | 56 | 0.0 | 3.0 | 2.00 | 0.79 | 56 | 0.0 | 3.0 | 1.34 | 0.90 |
| Triangles | 121 | 0.0 | 3.0 | 1.74 | 1.18 | 92 | 1.0 | 3.0 | 2.09 | 0.64 | 92 | 0.0 | 3.0 | 2.09 | 0.67 | 92 | 0.0 | 3.0 | 1.54 | 0.84 |
| Quadrilaterals | 121 | 0.0 | 3.0 | 1.18 | 1.20 | 67 | 1.0 | 3.0 | 2.04 | 0.66 | 67 | 0.0 | 3.0 | 2.09 | 0.67 | 67 | 0.0 | 3.0 | 1.54 | 0.77 |
| Other polygons | 121 | 0.0 | 3.0 | 0.64 | 0.92 | 47 | 0.0 | 3.0 | 1.77 | 0.79 | 47 | 0.0 | 3.0 | 1.74 | 0.71 | 47 | 0.0 | 3.0 | 1.34 | 0.87 |


|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | /l/P | form | oced |  |  | onst Un | $\begin{aligned} & \text { te/C } \\ & \text { rsta } \end{aligned}$ | mun <br> ing |  |  |  | ner |  |  |
| Pythagorean theorem | 121 | 0.0 | 3.0 | 1.36 | 1.05 | 85 | 1.0 | 3.0 | 2.21 | 0.71 | 85 | 0.0 | 3.0 | 1.86 | 0.73 | 85 | 0.0 | 3.0 | 1.67 | 0.86 |
| Right triangles | 122 | 0.0 | 3.0 | 1.83 | 1.14 | 97 | 1.0 | 3.0 | 2.05 | 0.62 | 97 | 0.0 | 3.0 | 2.00 | 0.75 | 97 | 0.0 | 3.0 | 1.73 | 0.82 |
| Circles (arc length and area) | 122 | 0.0 | 3.0 | 0.89 | 1.23 | 45 | 0.0 | 3.0 | 2.00 | 0.67 | 45 | 0.0 | 3.0 | 2.13 | 0.76 | 46 | 0.0 | 3.0 | 1.50 | 0.72 |
| Circles (chords, tangents, and secants) | 122 | 0.0 | 3.0 | 0.75 | 1.17 | 39 | 1.0 | 3.0 | 2.23 | 0.63 | 39 | 1.0 | 3.0 | 2.13 | 0.57 | 39 | 0.0 | 3.0 | 1.46 | 0.72 |
| 3-D relationships | 122 | 0.0 | 3.0 | 0.48 | 0.93 | 31 | 0.0 | 3.0 | 1.90 | 0.87 | 31 | 0.0 | 3.0 | 1.55 | 0.77 | 31 | 0.0 | 2.0 | 1.23 | 0.81 |
| Classifying and describing 3-D figures | 122 | 0.0 | 3.0 | 0.54 | 0.90 | 38 | 1.0 | 3.0 | 2.05 | 0.80 | 38 | 0.0 | 3.0 | 1.66 | 0.71 | 38 | 0.0 | 3.0 | 1.26 | 0.86 |
| Structure of 3-D figures | 122 | 0.0 | 3.0 | 0.36 | 0.75 | 26 | 0.0 | 3.0 | 1.81 | 0.85 | 26 | 0.0 | 3.0 | 1.38 | 0.80 | 27 | 0.0 | 3.0 | 1.19 | 0.79 |
| Polyhedra | 122 | 0.0 | 3.0 | 0.17 | 0.59 | 11 | 1.0 | 3.0 | 1.73 | 0.79 | 11 | 0.0 | 3.0 | 1.64 | 0.81 | 11 | 0.0 | 3.0 | 1.55 | 1.04 |
| Cylinders, cones, and spheres | 122 | 0.0 | 3.0 | 0.93 | 1.13 | 57 | 1.0 | 3.0 | 2.05 | 0.74 | 57 | 0.0 | 3.0 | 1.86 | 0.79 | 57 | 0.0 | 3.0 | 1.53 | 0.85 |
| Geometric constructions | 122 | 0.0 | 3.0 | 0.49 | 0.87 | 34 | 1.0 | 3.0 | 2.03 | 0.72 | 34 | 0.0 | 3.0 | 1.76 | 0.82 | 34 | 0.0 | 3.0 | 1.18 | 0.83 |
| Loci | 122 | 0.0 | 2.0 | 0.06 | 0.27 | 6 | 0.0 | 2.0 | 1.17 | 0.75 | 6 | 0.0 | 2.0 | 0.83 | 0.75 | 6 | 0.0 | 2.0 | 1.00 | 0.63 |
| Analytic or coordinate geometry | 122 | 0.0 | 3.0 | 0.78 | 1.09 | 45 | 1.0 | 3.0 | 1.96 | 0.56 | 45 | 0.0 | 3.0 | 2.04 | 0.82 | 45 | 0.0 | 3.0 | 1.60 | 0.78 |
| Symmetry | 122 | 0.0 | 3.0 | 0.85 | 0.98 | 61 | 1.0 | 3.0 | 1.79 | 0.73 | 61 | 0.0 | 3.0 | 1.75 | 0.81 | 62 | 0.0 | 3.0 | 1.31 | 0.97 |
| Geometric modeling | 122 | 0.0 | 3.0 | 0.60 | 0.99 | 37 | 1.0 | 3.0 | 1.70 | 0.66 | 37 | 0.0 | 3.0 | 1.84 | 0.73 | 37 | 0.0 | 3.0 | 1.84 | 0.90 |
| Geometric patterns | 122 | 0.0 | 3.0 | 0.22 | 0.62 | 17 | 1.0 | 3.0 | 1.76 | 0.83 | 17 | 0.0 | 3.0 | 1.71 | 0.77 | 17 | 0.0 | 3.0 | 1.47 | 1.01 |
| Non-Euclidian geometry | 122 | 0.0 | 3.0 | 0.09 | 0.43 | 6 | 1.0 | 2.0 | 1.67 | 0.52 | 6 | 1.0 | 3.0 | 1.83 | 0.75 | 6 | 1.0 | 3.0 | 1.83 | 0.75 |
| Topology | 122 | 0.0 | 3.0 | 0.04 | 0.33 | 2 | 2.0 | 2.0 | 2.00 | 0.00 | 2 | 2.0 | 2.0 | 2.00 | 0.00 | 2 | 2.0 | 2.0 | 2.00 | 0.00 |


|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recall/Perform Procedures |  |  |  |  | Demonstrate/Communicate Understanding |  |  |  |  | Generalize |  |  |  |  |
| Trigonometry |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| OVERALL | 121 | 0.0 | 3.0 | 0.89 | 0.74 | 94 | 1.0 | 3.0 | 2.04 | 0.63 | 94 | 0.0 | 3.0 | 1.90 | 0.61 | 94 | 0.0 | 3.0 | 1.49 | 0.75 |
| Basic ratios | 121 | 0.0 | 3.0 | 1.58 | 1.15 | 88 | 1.0 | 3.0 | 2.10 | 0.71 | 88 | 0.0 | 3.0 | 1.98 | 0.68 | 88 | 0.0 | 3.0 | 1.49 | 0.86 |
| Radian measure | 121 | 0.0 | 3.0 | 0.58 | 0.94 | 38 | 0.0 | 3.0 | 2.00 | 0.90 | 38 | 0.0 | 3.0 | 1.68 | 0.78 | 38 | 0.0 | 3.0 | 1.08 | 0.85 |
| Right-triangle trigonometry | 121 | 0.0 | 3.0 | 1.60 | 1.31 | 78 | 1.0 | 3.0 | 2.18 | 0.70 | 78 | 0.0 | 3.0 | 2.04 | 0.61 | 78 | 0.0 | 3.0 | 1.77 | 0.87 |
| Law of Sines and Cosines | 121 | 0.0 | 3.0 | 0.75 | 1.10 | 43 | 1.0 | 3.0 | 2.26 | 0.69 | 43 | 0.0 | 3.0 | 1.88 | 0.73 | 43 | 0.0 | 3.0 | 1.56 | 0.88 |
| Identities | 121 | 0.0 | 3.0 | 0.38 | 0.76 | 29 | 1.0 | 3.0 | 1.83 | 0.71 | 29 | 0.0 | 3.0 | 1.72 | 0.75 | 29 | 0.0 | 3.0 | 1.28 | 0.88 |
| Trigonometric equations | 121 | 0.0 | 3.0 | 0.48 | 0.97 | 27 | 1.0 | 3.0 | 1.96 | 0.81 | 27 | 0.0 | 3.0 | 1.78 | 0.70 | 27 | 0.0 | 3.0 | 1.52 | 0.85 |

The following tables show the average level of coverage and cognitive demand emphasis for teachers who identified Integrated Math II as their target math class. The first table presents these data for all IM II teachers, while the second table shows IM II teachers' average level of coverage by the achievement level of students in their target math class.

Average Level of Coverage \& Cognitive Demand Emphasis by Math Domain for Integrated Math II Teachers Only

|  | Level of Coverage |  |  |  |  | Cognitive Demand Emphasis |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recall/Perform Procedures |  |  |  |  | Demonstrate/Communicate Understanding |  |  |  |  | Generalize |  |  |  |  |
| Math Domain | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD | N | Min | Max | Mean | SD |
| Number Properties \& Operations | 48 | 0.1 | 3.0 | 1.78 | 0.68 | 48 | 0.5 | 3.0 | 1.81 | 0.50 | 48 | 0.5 | 3.0 | 1.75 | 0.56 | 48 | 0.0 | 3.0 | 1.53 | 0.62 |
| Basic Algebra | 48 | 0.7 | 2.8 | 2.03 | 0.47 | 48 | 1.0 | 2.9 | 1.89 | 0.46 | 48 | 1.0 | 2.8 | 1.93 | 0.44 | 48 | 0.4 | 3.0 | 1.63 | 0.60 |
| Advanced Algebra | 47 | 0.5 | 2.5 | 1.21 | 0.42 | 47 | 1.0 | 3.0 | 2.07 | 0.44 | 47 | 0.63 | 2.67 | 1.91 | 0.44 | 47 | 0.0 | 3.0 | 1.47 | 0.76 |
| Functions | 47 | 0.3 | 2.5 | 1.30 | 0.52 | 47 | 1.0 | 2.6 | 1.82 | 0.43 | 47 | 0.8 | 3.0 | 1.90 | 0.50 | 47 | 0.0 | 3.0 | 1.57 | 0.71 |
| Geometric Concepts | 47 | 0.0 | 2.1 | 0.91 | 0.45 | 46 | 1.0 | 2.8 | 1.84 | 0.49 | 46 | 0.1 | 3.0 | 1.90 | 0.53 | 46 | 0.0 | 3.0 | 1.4 | 0.72 |
| Trigonometry | 47 | 0.3 | 2.5 | 1.13 | 0.49 | 47 | 1.0 | 3.0 | 2.11 | 0.61 | 47 | 0.0 | 3.0 | 1.92 | 0.55 | 47 | 0.0 | 3.0 | 1.56 | 0.77 |

Note. 1 teacher only completed the "Number Properties \& Operations" and "Basic Algebra" sections. Another teacher chose " 0 " for level of coverage on all Geometry items.

## Average Level of Coverage in Integrated Math II Classes by Achievement Level of Target Math Class

|  | Achievement Level of Target Math Class |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | High ( $\mathrm{N}=6$ ) |  |  |  | Average ( $\mathrm{N}=7$ ) |  |  |  | Low ( $\mathrm{N}=16$ ) |  |  |  | Mixed ( $\mathrm{N}=19$ ) |  |  |  |
| Math Domain | Min | Max | Mean | SD | Min | Max | Mean | SD | Min | Max | Mean | SD | Min | Max | Mean | SD |
| Number Properties \& Operations | 0.1 | 3.0 | 1.81 | 1.05 | 0.3 | 2.9 | 1.75 | 0.86 | 0.6 | 3.0 | 1.85 | 0.59 | 0.6 | 2.8 | 1.72 | 0.60 |
| Basic Algebra | 1.5 | 2.7 | 2.18 | 0.51 | 1.7 | 2.8 | 2.25 | 0.42 | 1.3 | 2.8 | 2.05 | 0.43 | 0.7 | 2.7 | 1.89 | 0.48 |
| Advanced Algebra | 1.1 | 2.0 | 1.40 | 0.33 | 0.6 | 1.9 | 1.20 | 0.49 | 0.5 | 2.5 | 1.20 | 0.53 | 0.7 | 1.9 | 1.17 | 0.33 |
| Functions | 1.0 | 2.5 | 1.63 | 0.56 | 0.4 | 1.8 | 1.12 | 0.49 | 0.8 | 2.4 | 1.38 | 0.46 | 0.3 | 2.1 | 1.20 | 0.54 |
| Geometric Concepts | 0.7 | 2.1 | 1.30 | 0.47 | 0.0 | 1.1 | 0.78 | 0.42 | 0.1 | 1.7 | 0.90 | 0.49 | 0.4 | 1.8 | 0.83 | 0.37 |
| Trigonometry | 0.8 | 2.3 | 1.36 | 0.59 | 0.3 | 1.3 | 0.81 | 0.37 | 0.5 | 1.7 | 1.22 | 0.40 | 0.5 | 2.5 | 1.10 | 0.53 |

Note. 1 teacher in the "Mixed" category only completed the "Number Properties \& Operations" and "Basic Algebra" sections of the survey.


[^0]:    *Grade level if not retained.

[^1]:    Note. 1 parent did not answer these interview questions.

[^2]:    Note. 1 parent did not answer these interview questions.

[^3]:    Note. 2 parents did not answer this question.

[^4]:    Note. 2 parents did not answer this question.

